



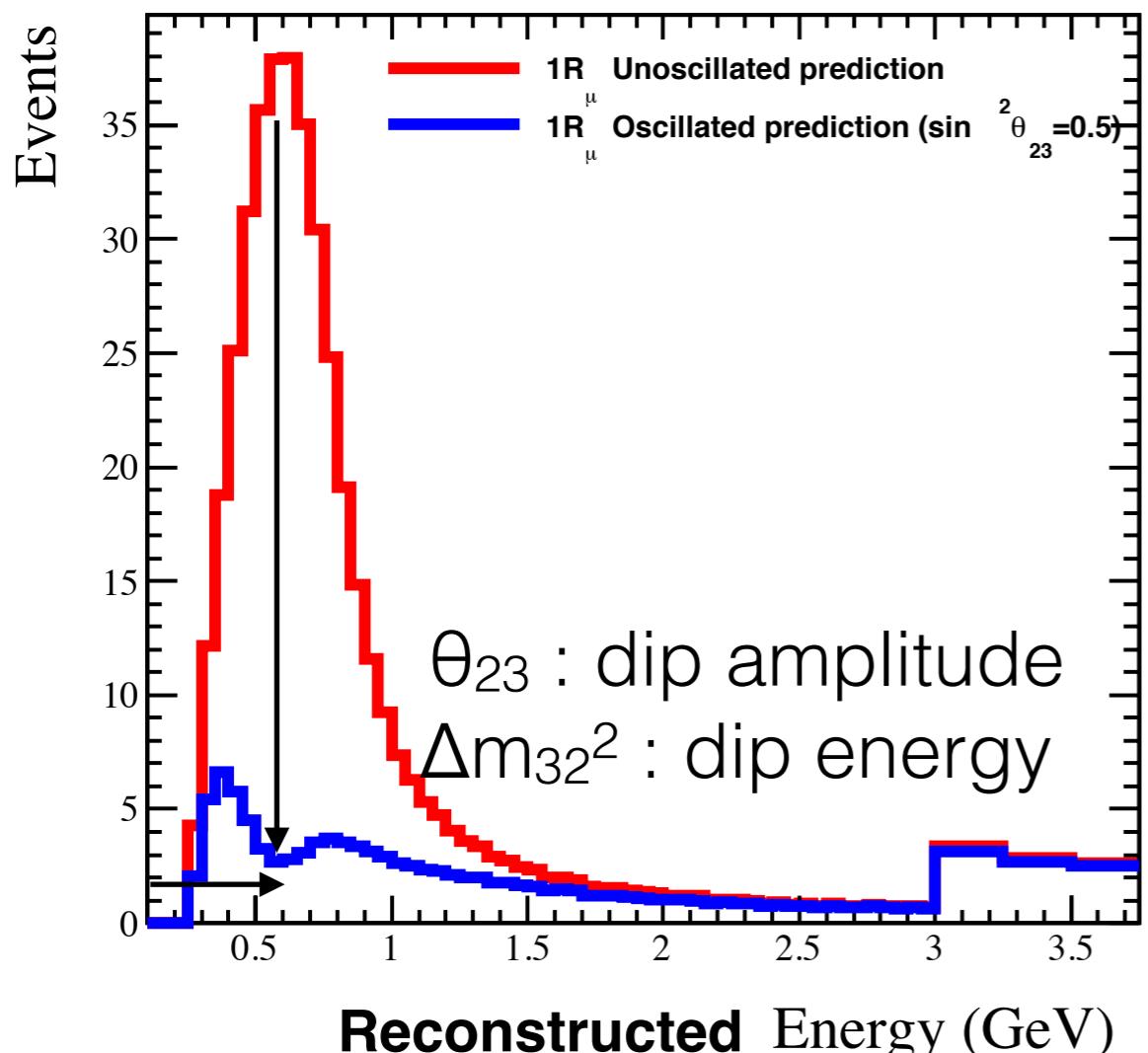
# Systematic Uncertainties in Long Baseline Neutrino Oscillation Measurements



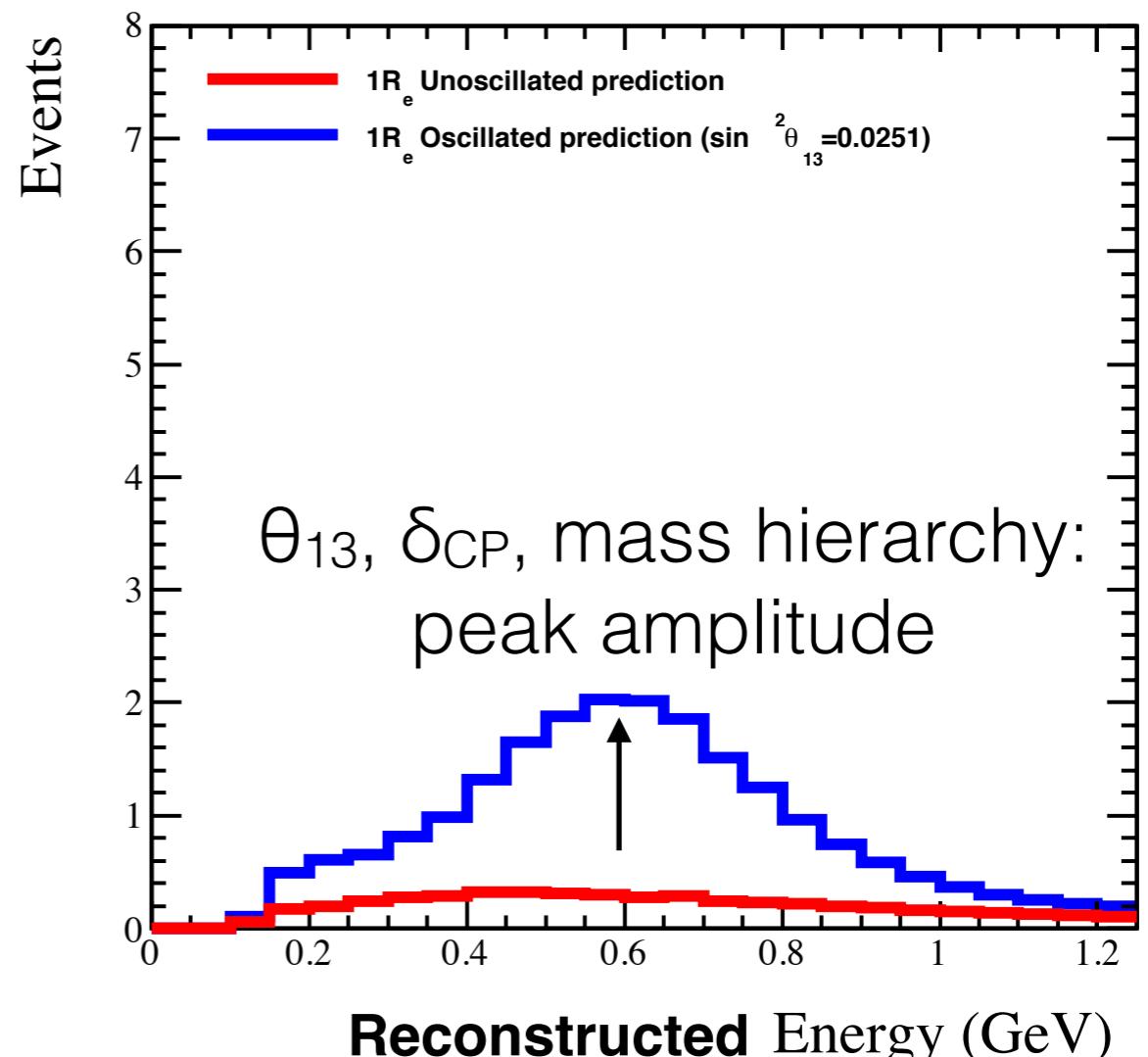
David Hadley  
21st December 2017  
Prospects in Neutrino Physics, NuPhys2017

# What is measured?

$\nu_\mu$  disappearance



$\nu_e$  appearance



Measurement precision limited by:

- Statistics
- Neutrino energy reconstruction
- Knowledge of unoscillated spectrum and background contamination

# Where do systematic uncertainties enter?



$$R(\vec{x}_{\text{reco}}) = \int \Phi(E_\nu) \times \sigma(E_\nu, \vec{x}_{\text{true}}) \times \varepsilon(\vec{x}_{\text{true}}, \vec{x}_{\text{reco}}) \times P(E_\nu, \vec{\theta}) dE_\nu d\vec{x}_{\text{true}}$$

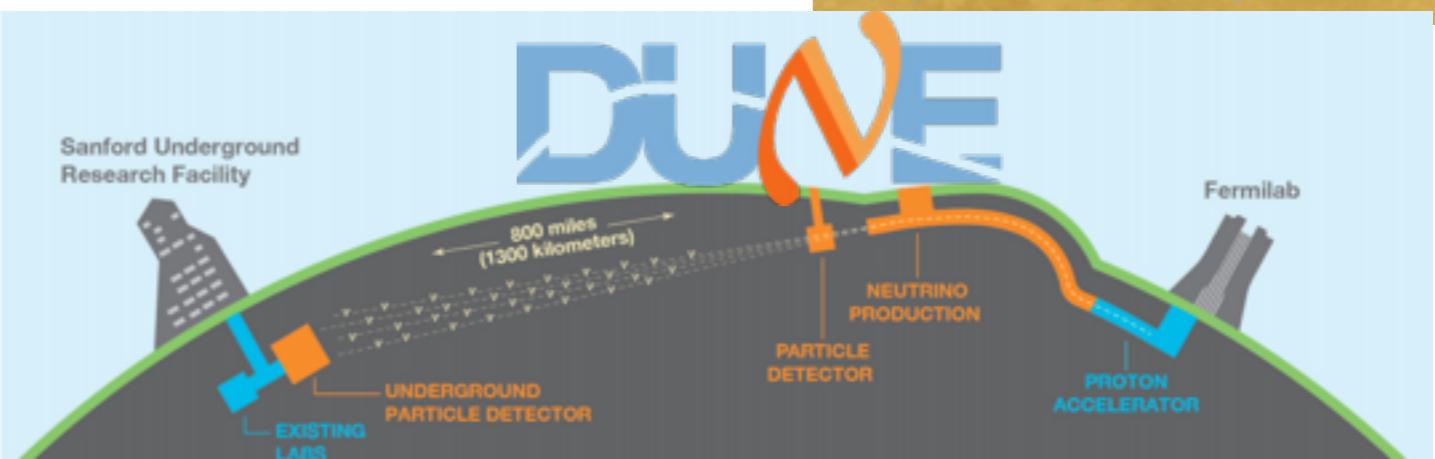
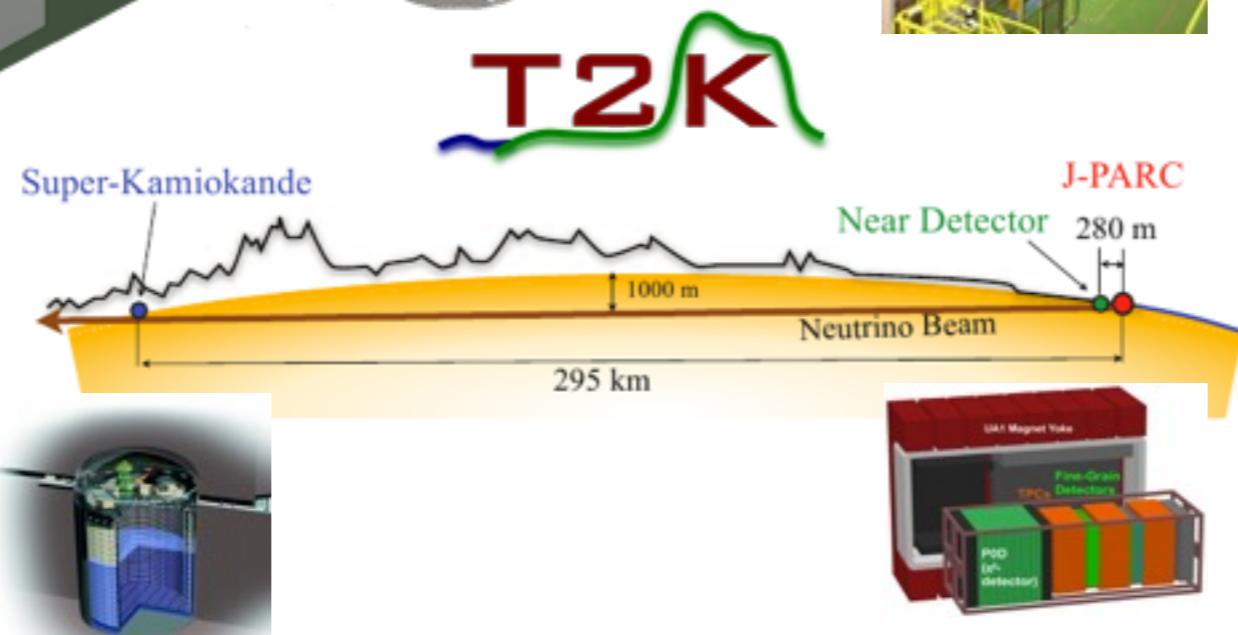
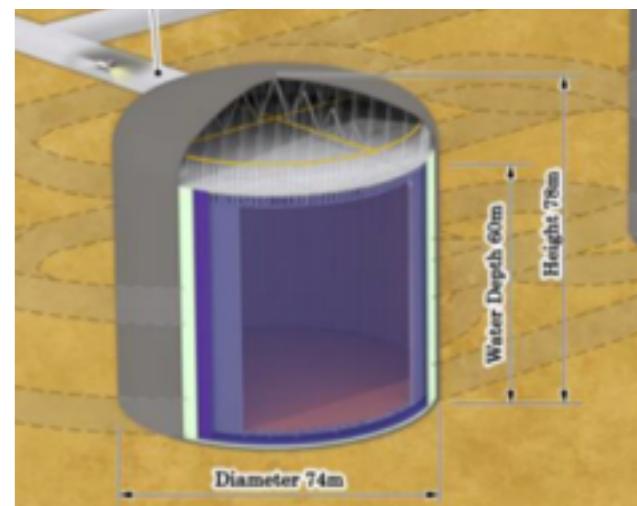
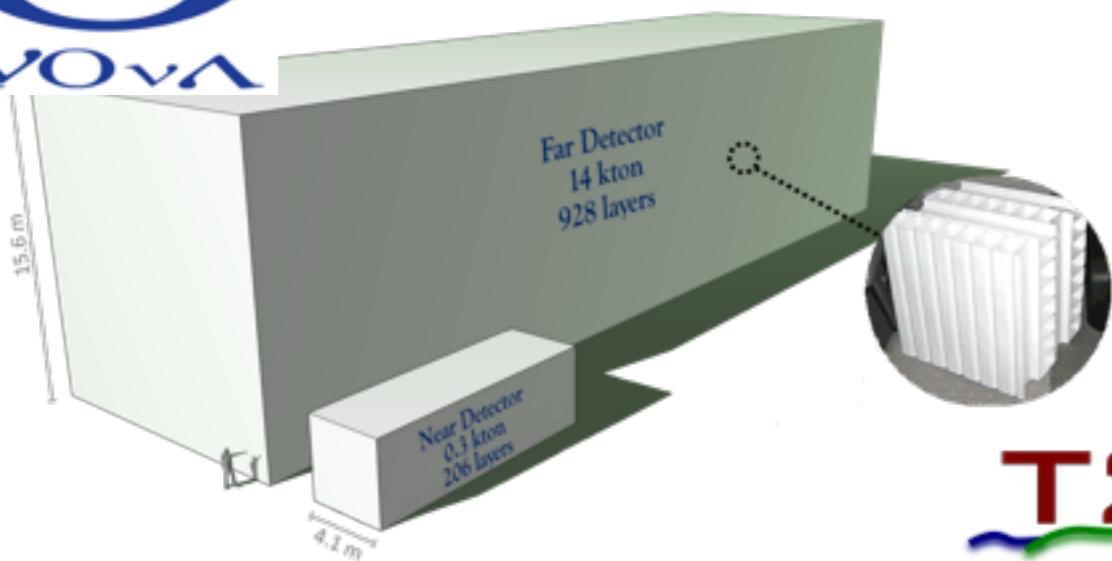
Neutrino Flux      Neutrino nucleus interaction model      Detector efficiency and resolution      Oscillation Probability

Four arrows point from the text labels below the equation to the terms in the equation above them: 'Neutrino Flux' points to  $\Phi(E_\nu)$ , 'Neutrino nucleus interaction model' points to  $\sigma(E_\nu, \vec{x}_{\text{true}})$ , 'Detector efficiency and resolution' points to  $\varepsilon(\vec{x}_{\text{true}}, \vec{x}_{\text{reco}})$ , and 'Oscillation Probability' points to  $P(E_\nu, \vec{\theta})$ .

Use measurements at near detector to constrain  $(\Phi \times \sigma \times \varepsilon)$

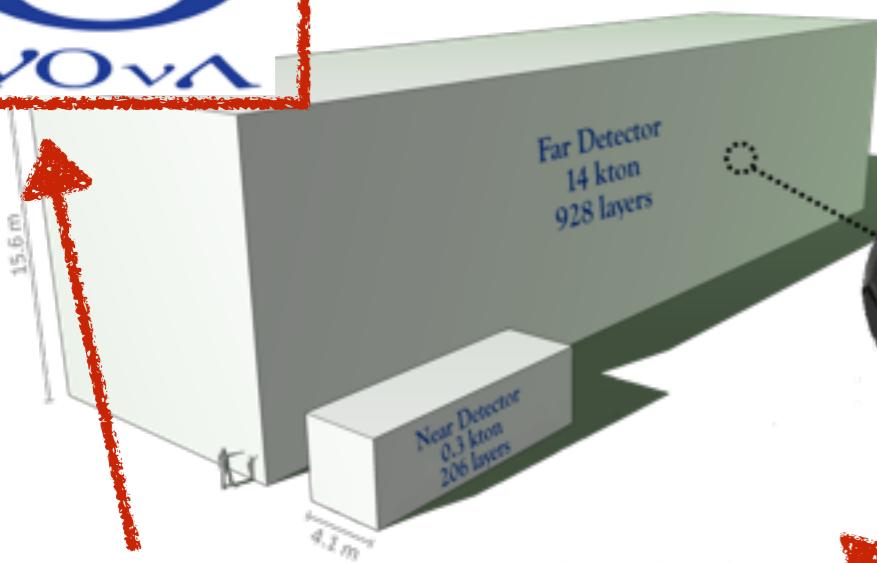
Cancellation of uncertainties is not perfect as no oscillation at the near detector and  $\Phi$  and  $\varepsilon$  may differ

# Accelerator based Neutrino Oscillation Experiments

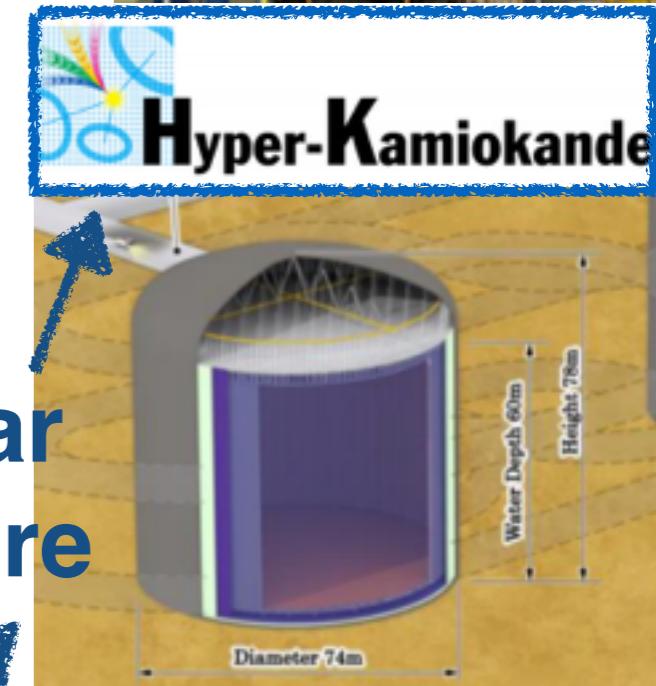
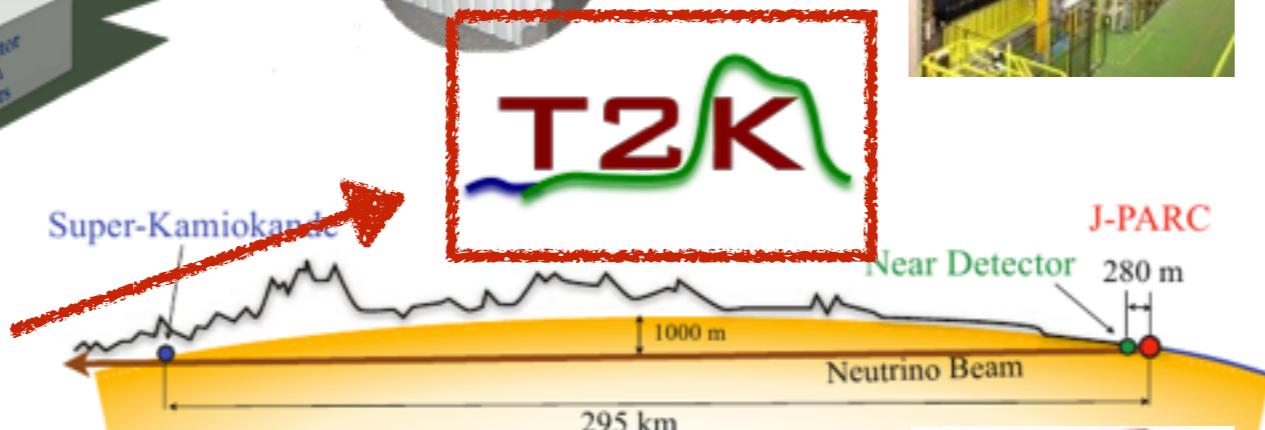


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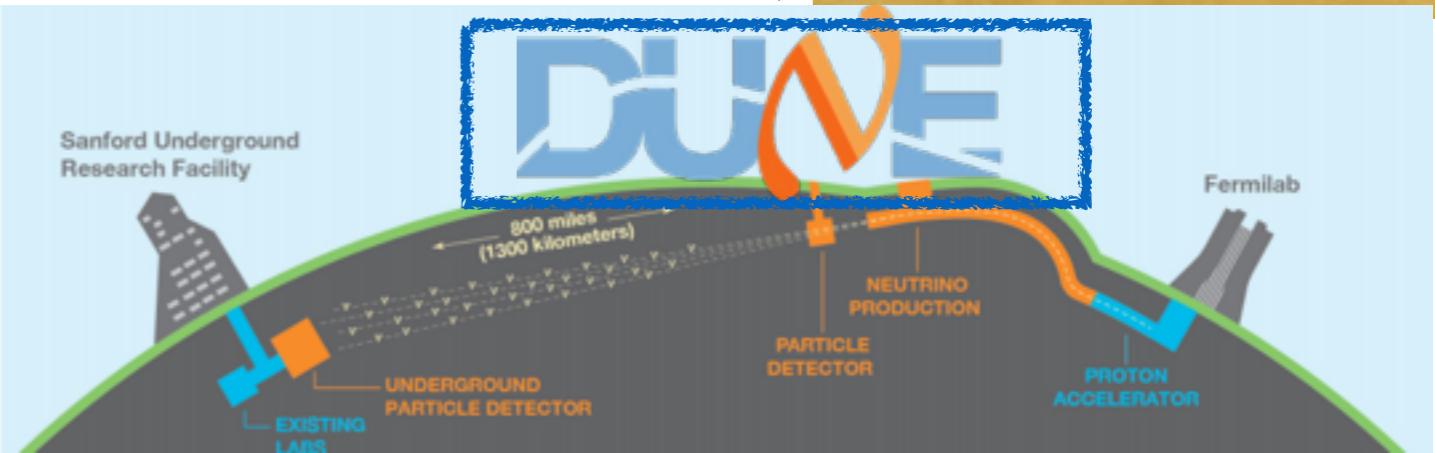
# Accelerator based Neutrino Oscillation Experiments



**Currently  
running long  
baseline  
experiments**



**Near  
future**



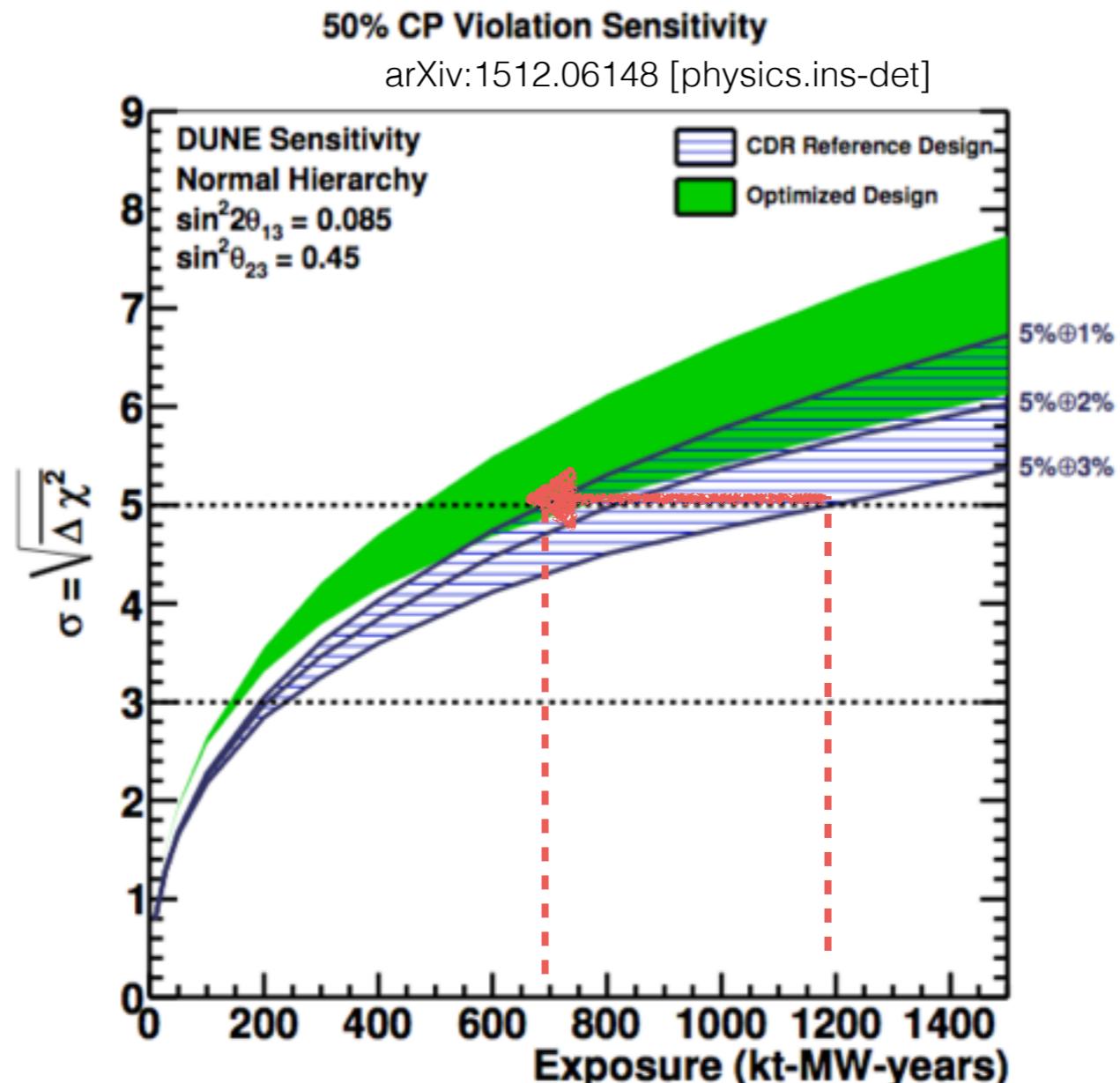
# Statistics



Experiment	$\nu_e + \bar{\nu}_e$	$1/\sqrt{N}$	Ref.
T2K (current)	74 + 7	12% + 40%	$2.2 \times 10^{21}$ POT
NOvA (current)	33	17%	FERMILAB-PUB-17-065-ND
NOvA (projected)	110 + 50	10% + 14%	arXiv:1409.7469 [hep-ex]
T2K-I (projected)	150 + 50	8% + 14%	$7.8 \times 10^{21}$ POT, arXiv:1409.7469 [hep-ex]
T2K-II	470 + 130	5% + 9%	$20 \times 10^{21}$ POT, arXiv:1607.08004 [hep-ex]
Hyper-K	2900 + 2700	2% + 2%	10 yrs 2-tank staged KEK Preprint 2016-21
DUNE	1200 + 350	3% + 5%	$3.5+3.5$ yrs x 40kt @ 1.07 MW arXiv:1512.06148 [physics.ins-det]

Current appearance measurements stats dominate  
 $O(10^3) \nu_e$  at future experiments  $\rightarrow$  demands  $\sim 2\%$  systematics  
 $O(10^4) \nu_\mu \rightarrow$  need systematics as good as we can get!

# Systematic Uncertainties



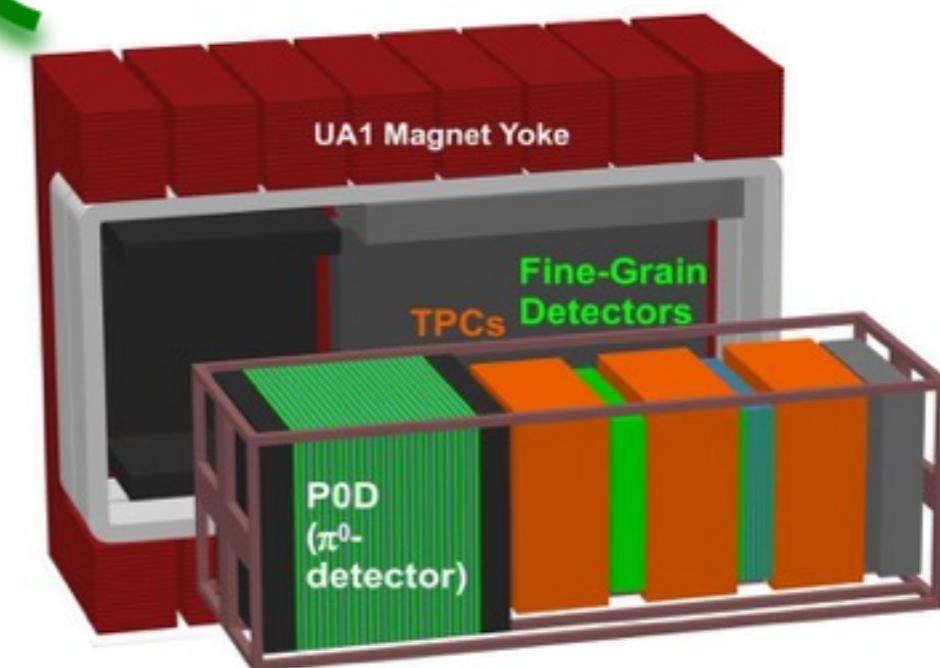
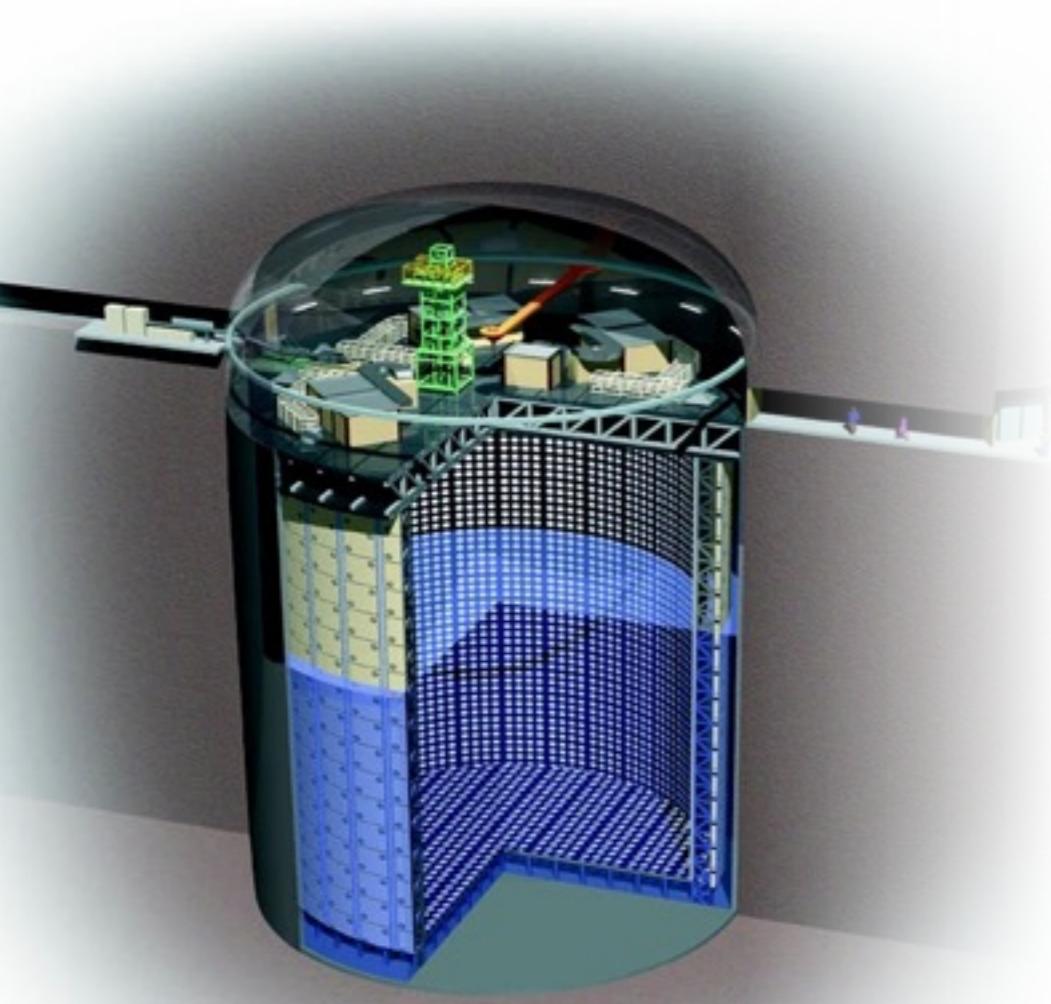
Reduction in systematic uncertainties  
can be equivalent to significant boost  
in exposure



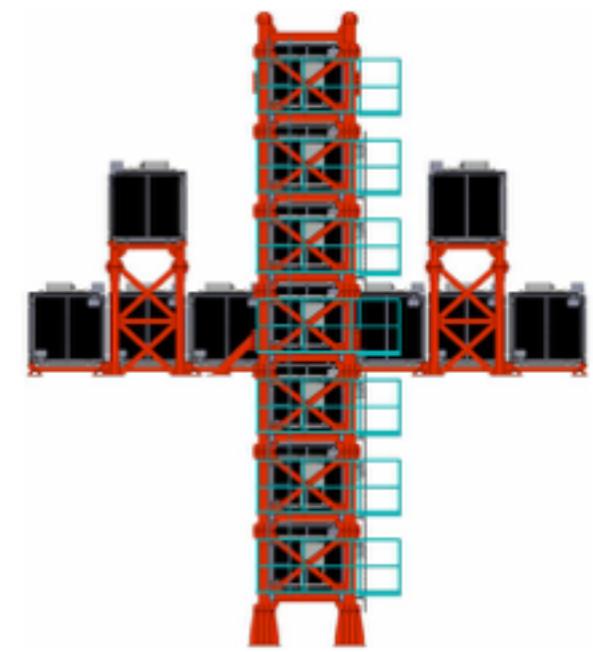
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Far Detector  
(Super-K)



Near Detectors  
(ND280+INGRID)

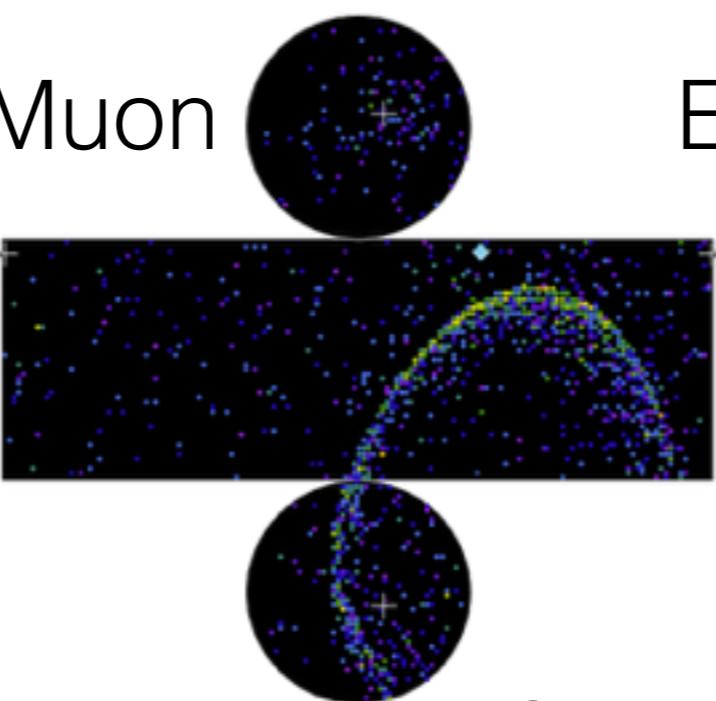




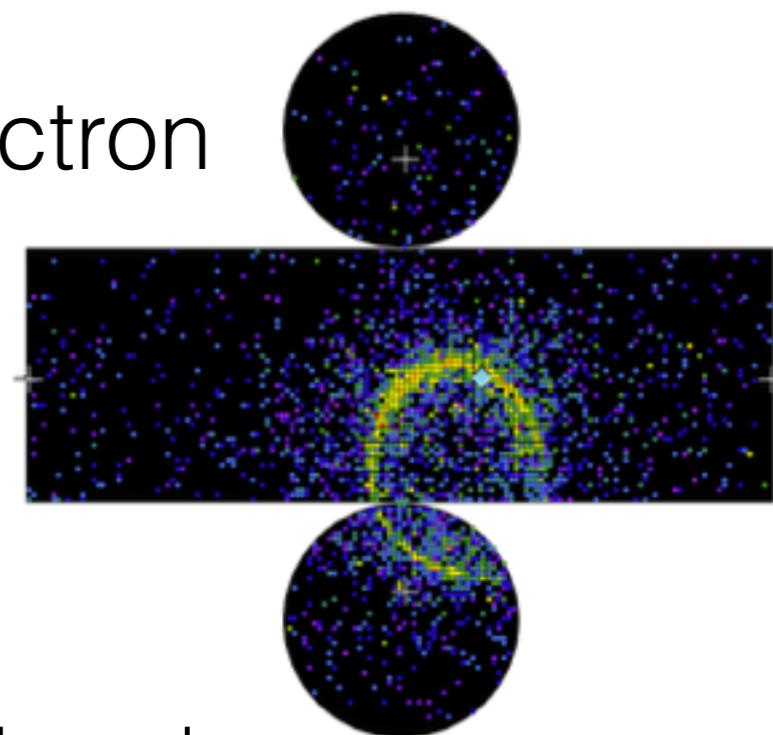
Water Cherenkov Far Detector  
>22.5 kt fiducial mass



Muon



Electron



Oxygen target  
 $4\pi$  acceptance

Energy reconstruction from lepton kinematics

Blind to particles below Cherenkov threshold  
for protons  $< 1.1 \text{ GeV}/c$ .  
(neutron counting possible with SK-Gd)

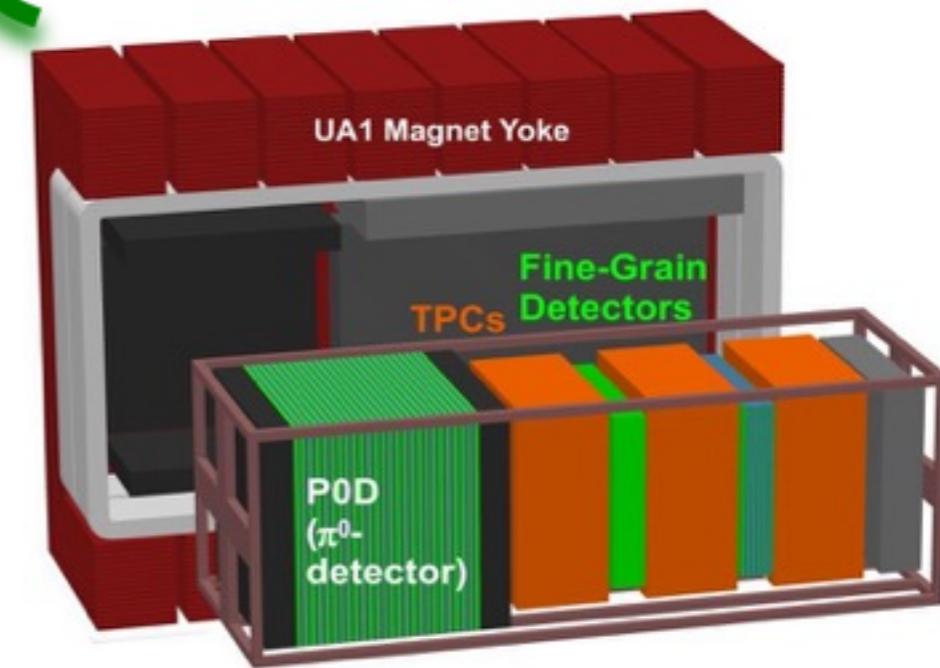


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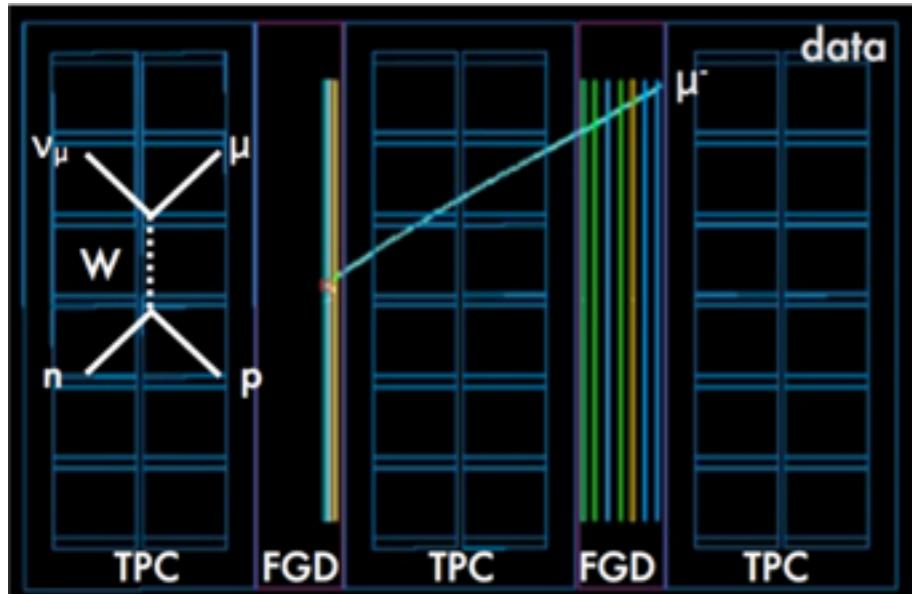
Carbon and Oxygen target materials

Acceptance differs from far detector

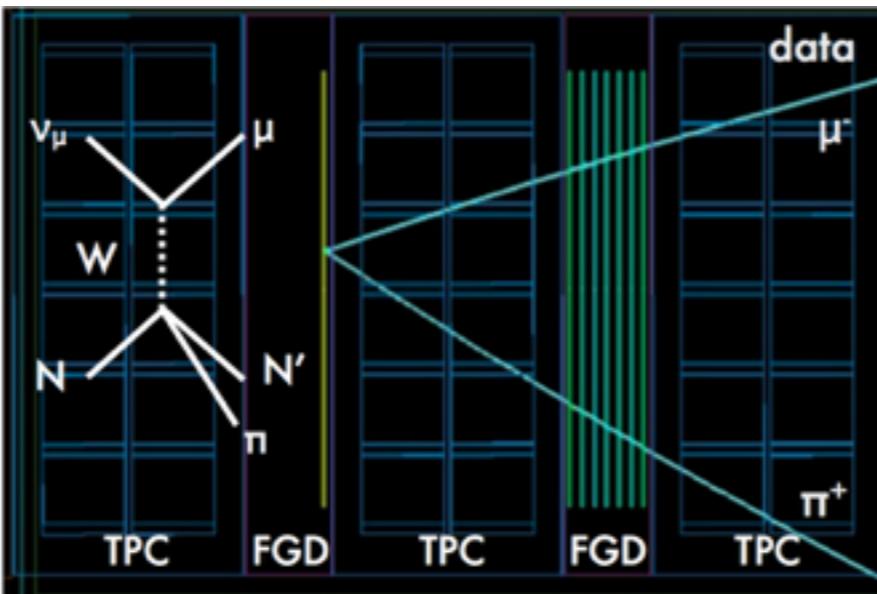
Magnetic field for sign selection



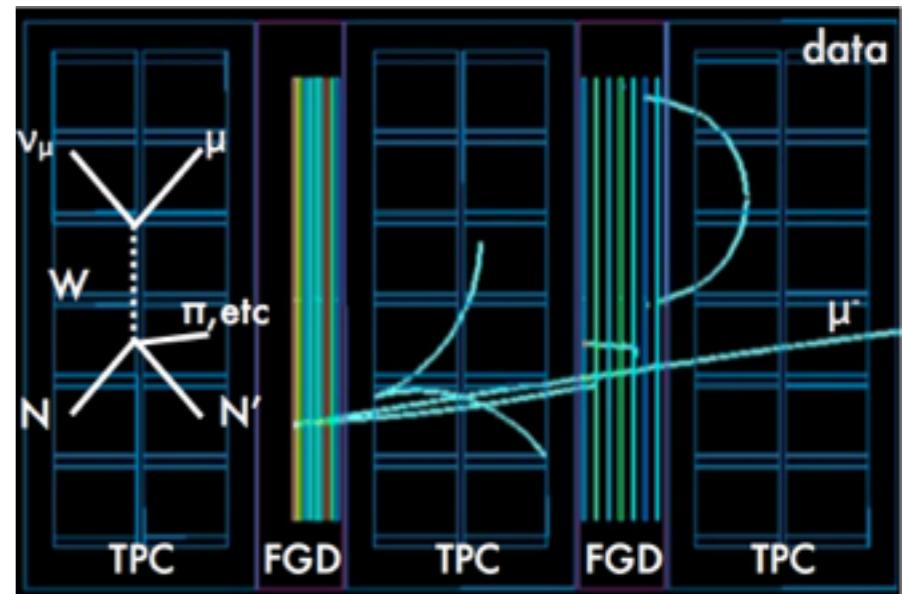
Near Detector (ND280)



CC 1 $\mu$  + 0 $\pi$  + X

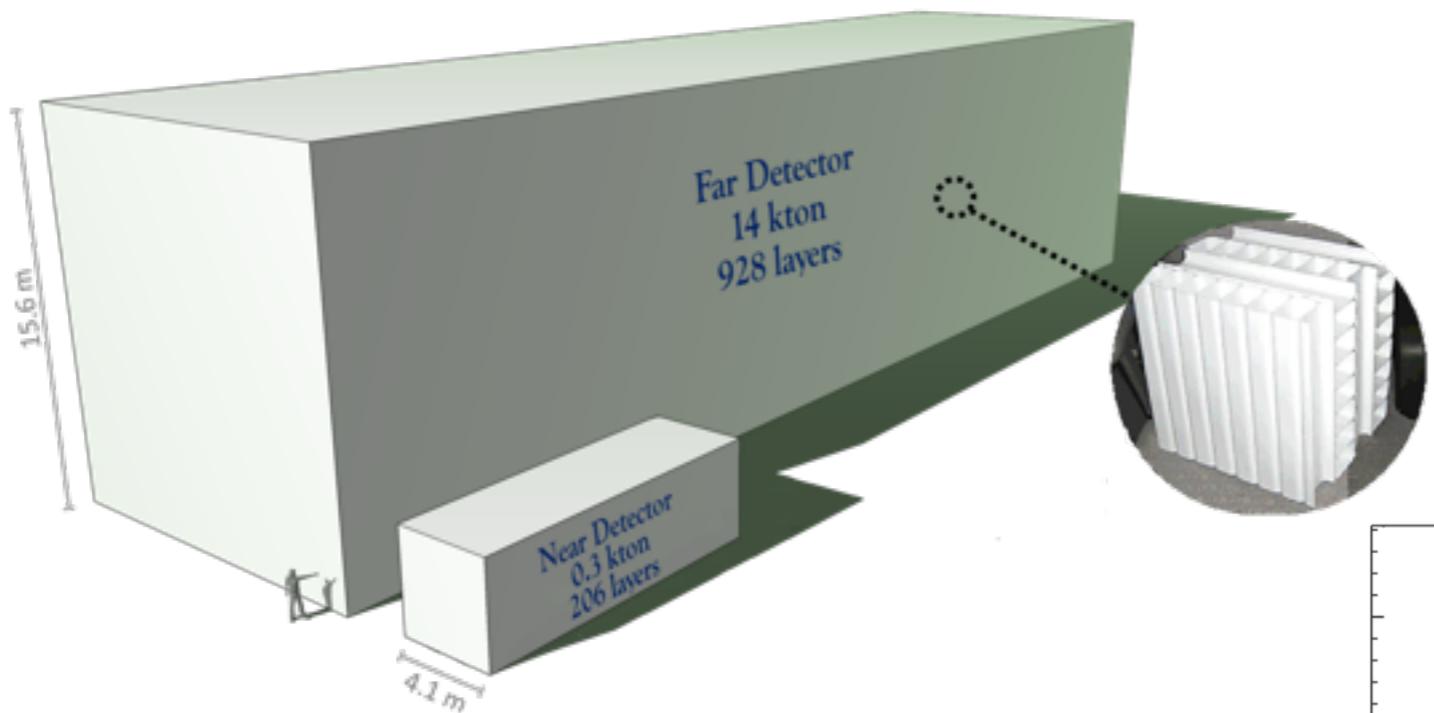


CC 1 $\mu$  + 1 $\pi^+$  + X



CC other

# NOvA Experiment

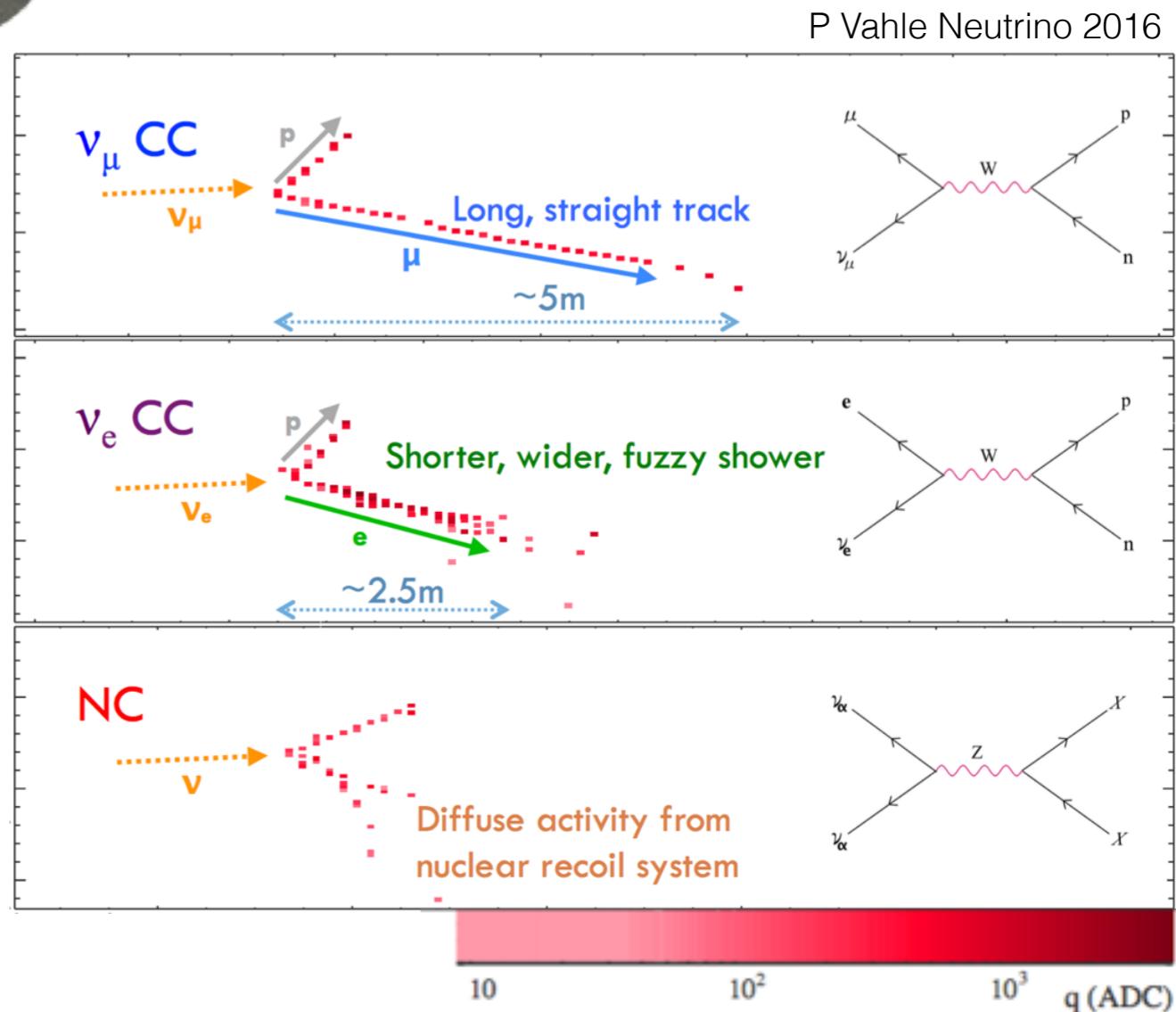


Liquid Scintillator tracking calorimeter

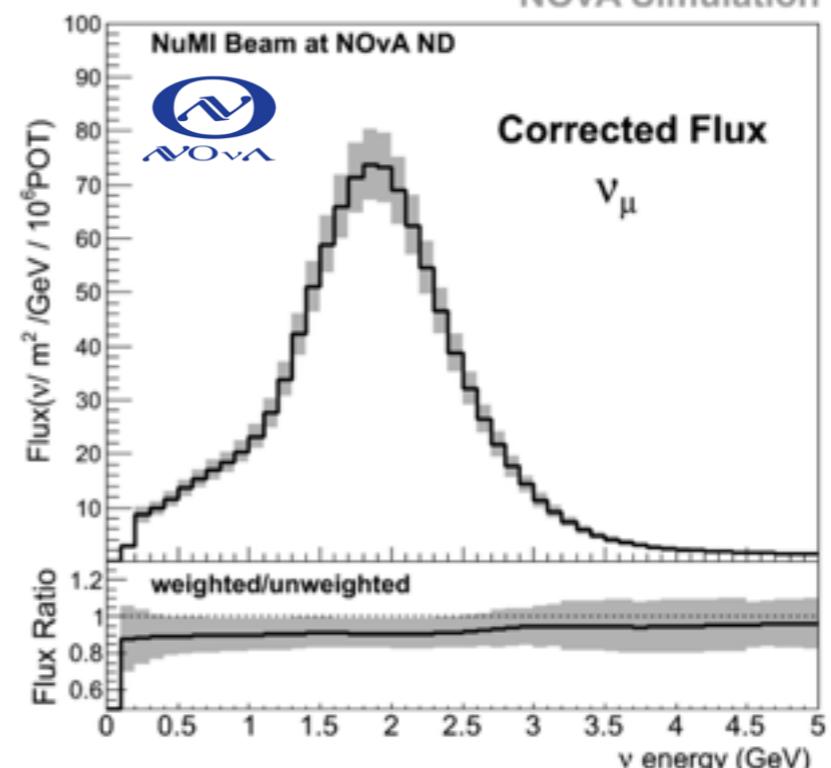
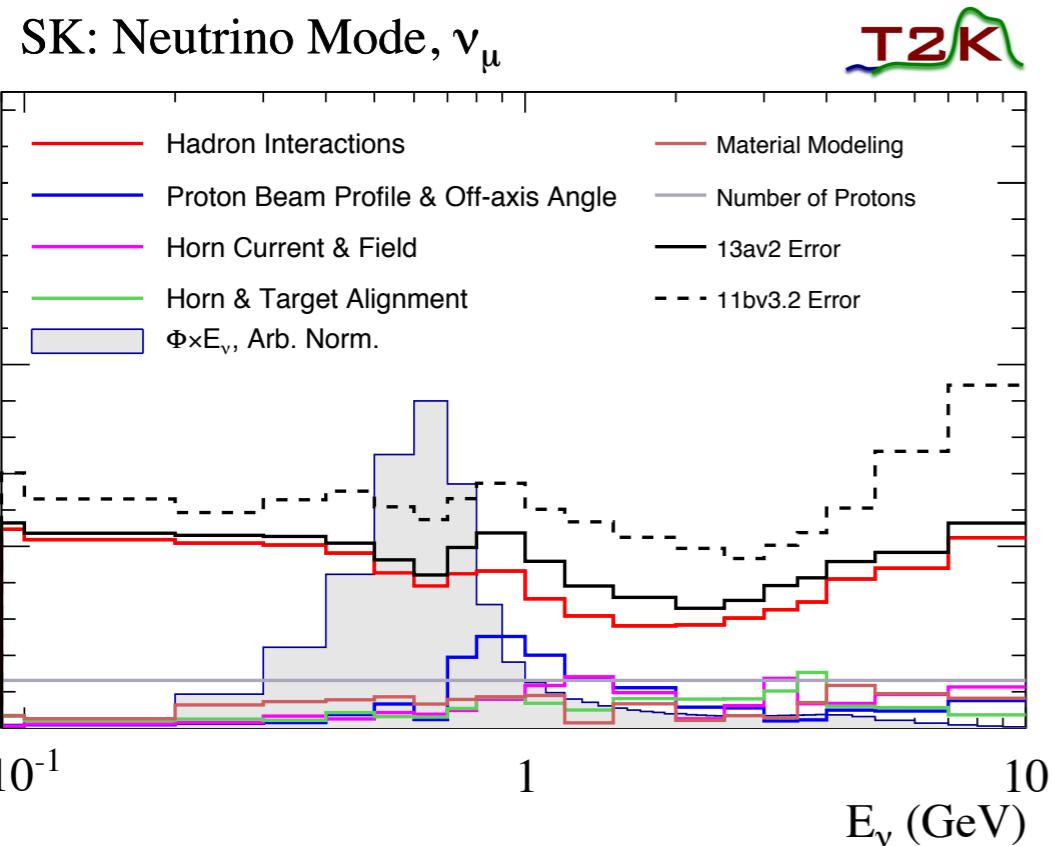
Almost identical near far detectors

Calorimetric Energy Reconstruction

$$E_{\nu \text{ reco}} = E_{\text{elep}} + E_{\text{had}}$$



# Flux Uncertainties



T2K ~ 8-12% (based on thin target tuning)

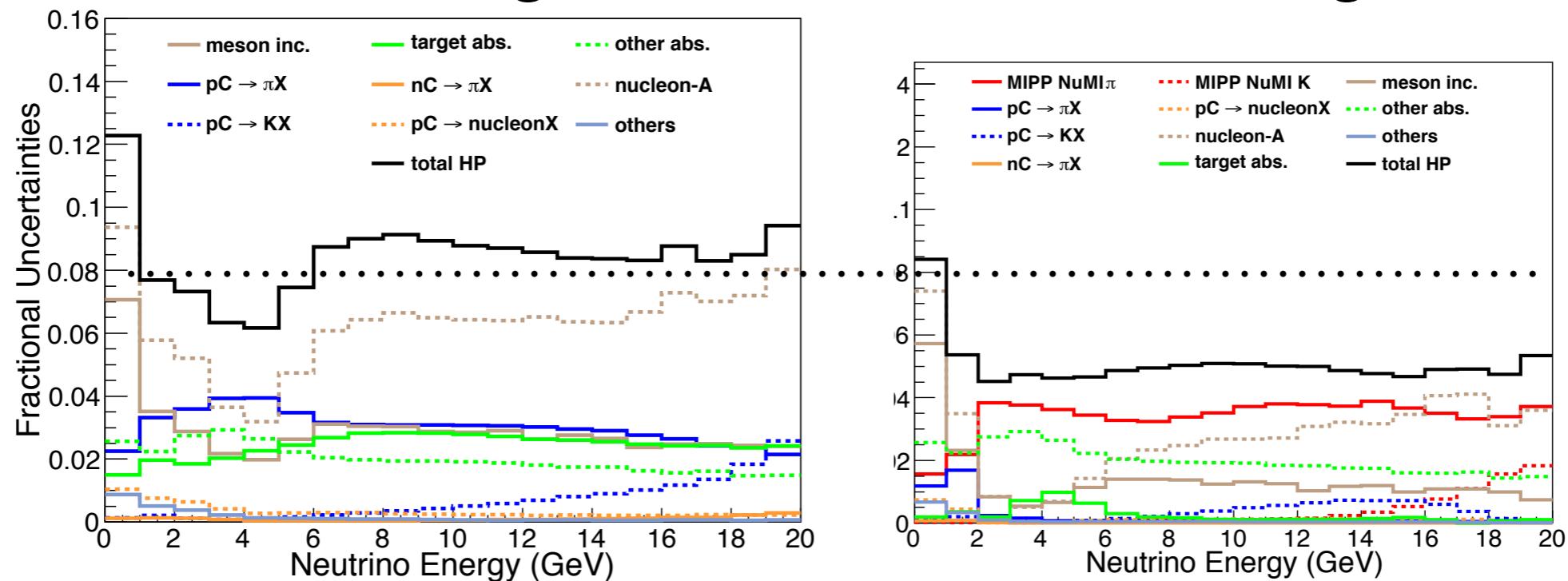
Dominated by hadron interaction modelling

Alignment/focussing uncertainties are also important  
(especially for near to far extrapolation)

# Flux Uncertainties

Thin Target

Thick Target



MINERvA Low E NuMI Flux Uncertainties, Phys. Rev. D 95, 039903 (2017)

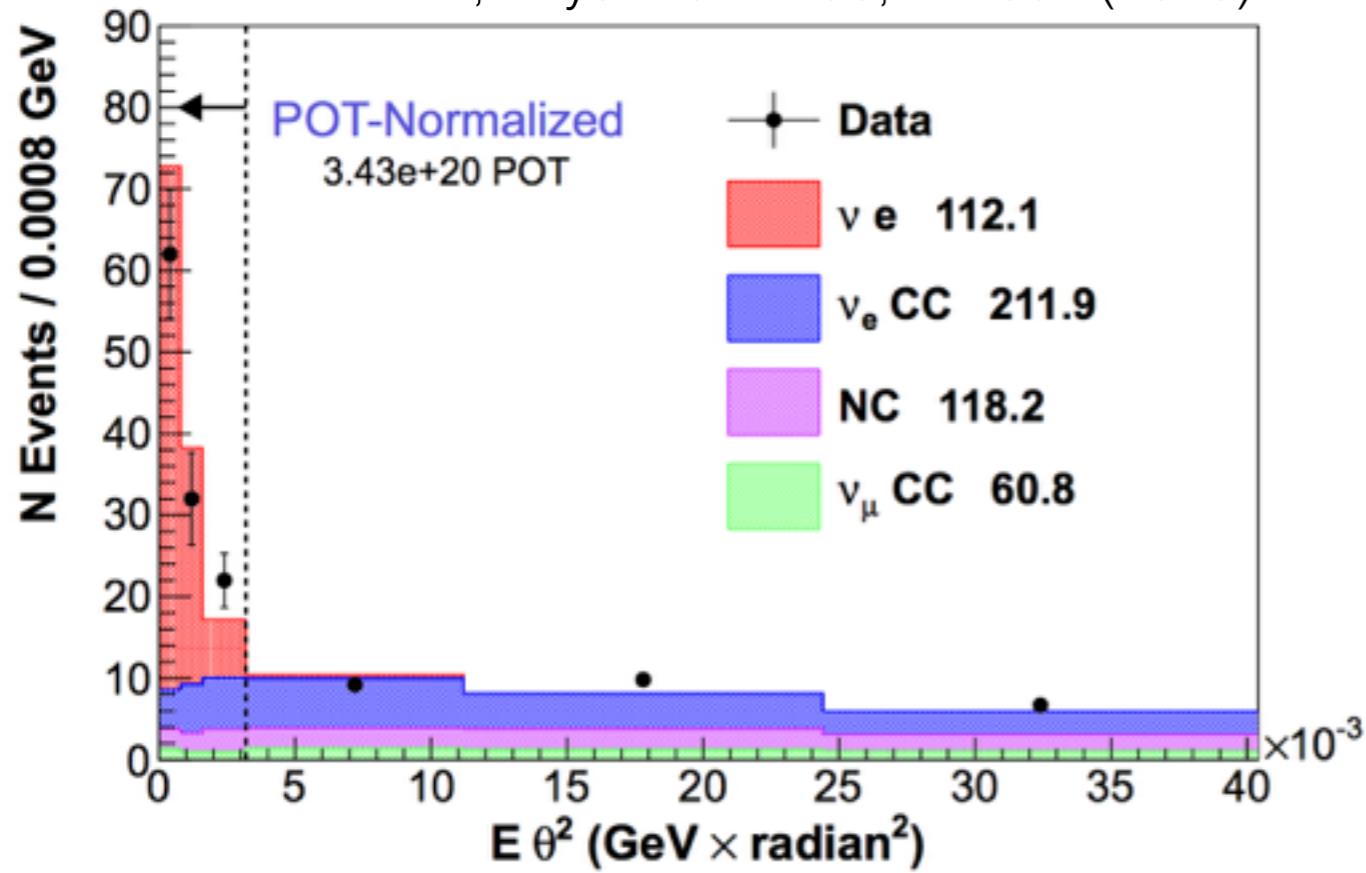
Significant reductions from thick/replica target  
 (See Tomislav Vladisavljevic poster for latest T2K tuning)

Future high beam power experiments may have different target material/geometry requiring dedicated hadron production measurements

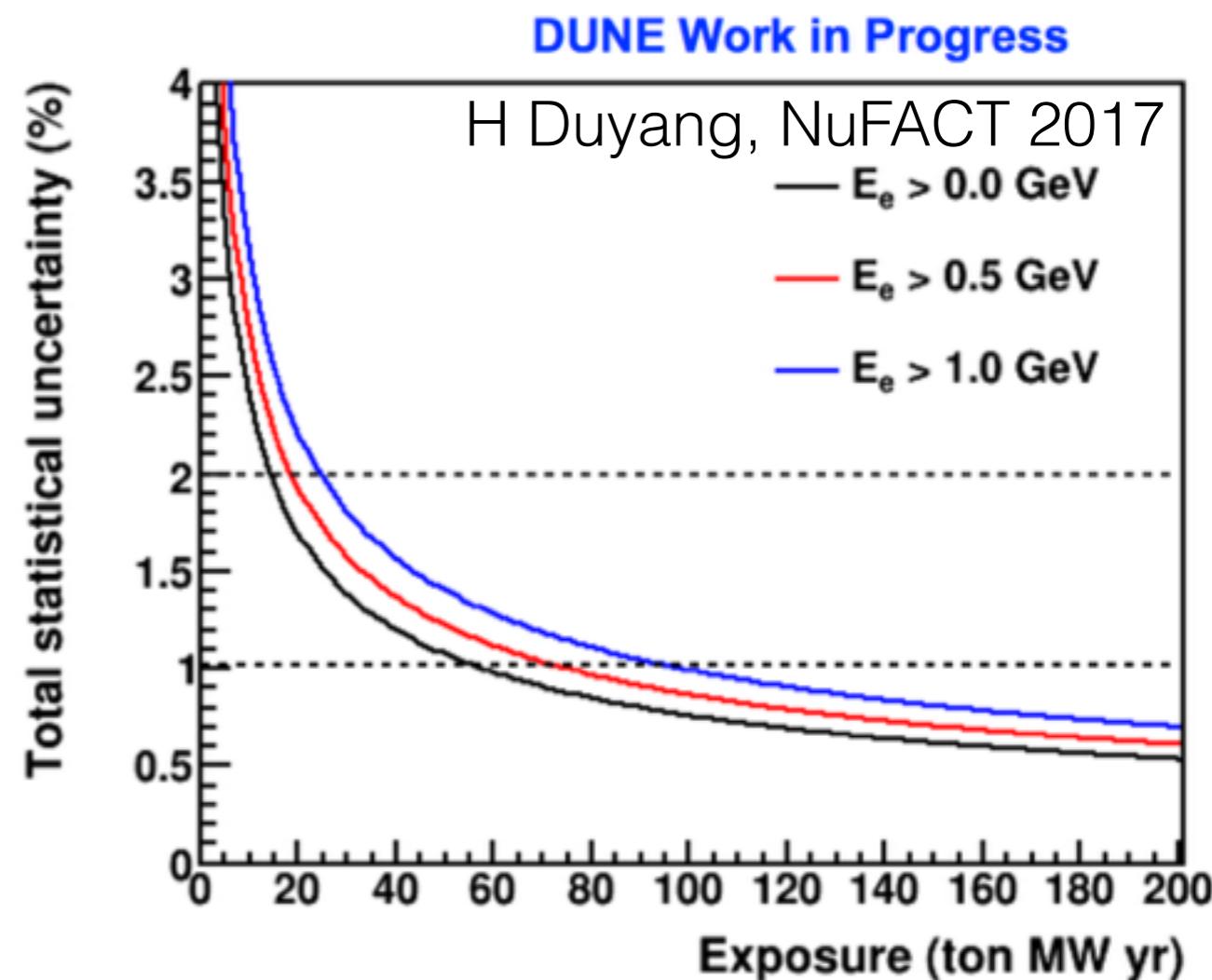
# Flux Uncertainties

In situ flux measurements possible  
eg neutrino-electron elastic scattering

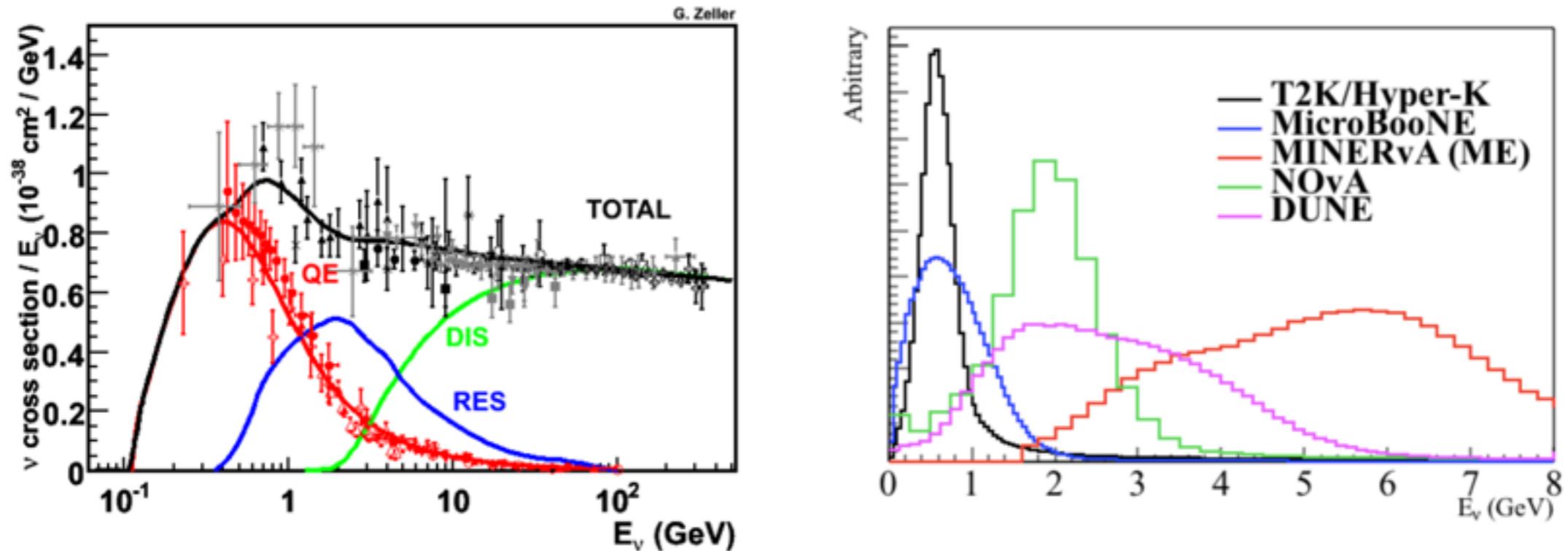
MINERvA, Phys. Rev. D 93, 112007 (2016)



DUNE Work in Progress



# Neutrino Interaction Model Uncertainties



Wide range of processes need to be simulated  
Require both lepton and hadronic side of the interaction  
Nuclear effects important in the relevant energy regime  
Experiments rely on MC generators  
for  $E_{\text{visible}} \rightarrow E_\nu$  extrapolation

Model parameter uncertainties from fits to external datasets

Sometimes parameter error must be inflated or ad-hoc parameters to account  
for discrepancies between model and data or known flaws in the model



# T2K Cross-Section Model

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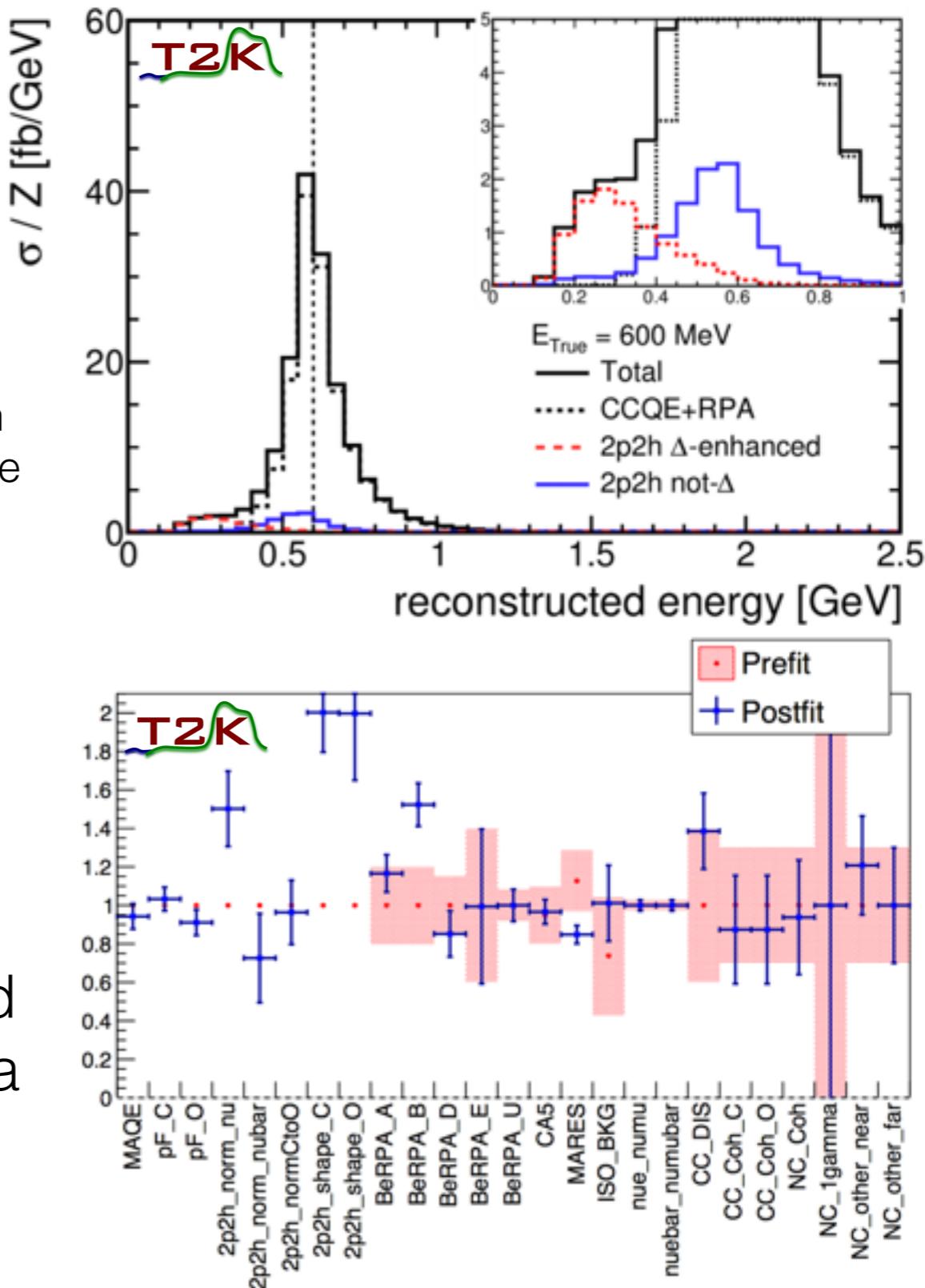
Implemented in NEUT MC generator

Quasi-elastic scattering most important process at T2K energies

- Valencia 2p-2h model Phys. Rev. C83 (2011) 045501
- Long-range effects with Random Phase Approximation
- Parameters introduced to vary normalisation and shape
- Relativistic Fermi Gas (RFG) nuclear model
- Uncertainties from RFG  $\leftrightarrow$  Local Fermi Gas
- Final state interactions with cascade model

No priors on most CCQE parameters  
Constraint from near detector

Impact of alternative models not implemented in oscillation analysis evaluated with fake data studies





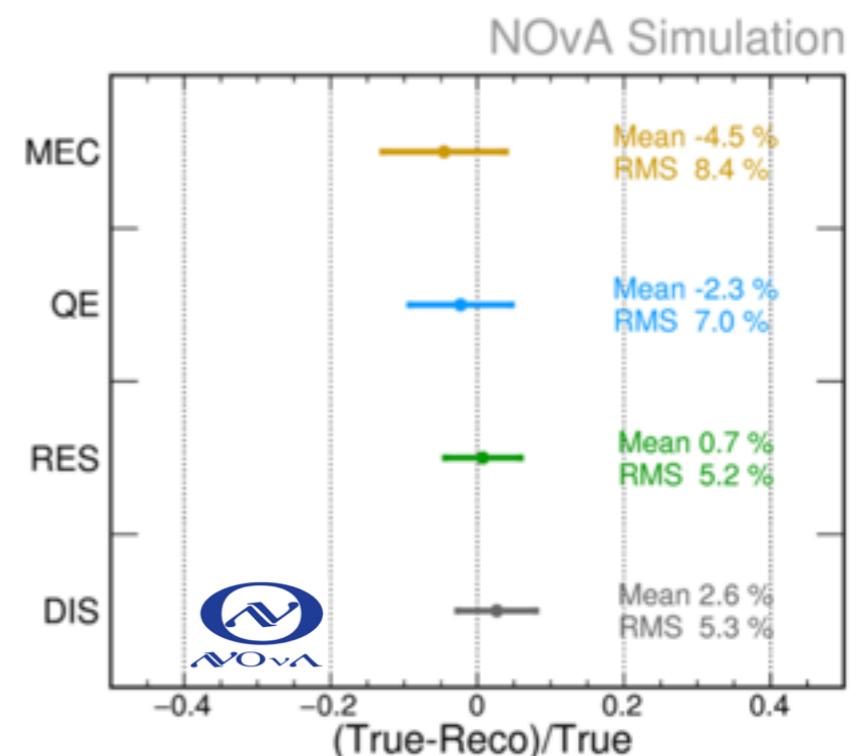
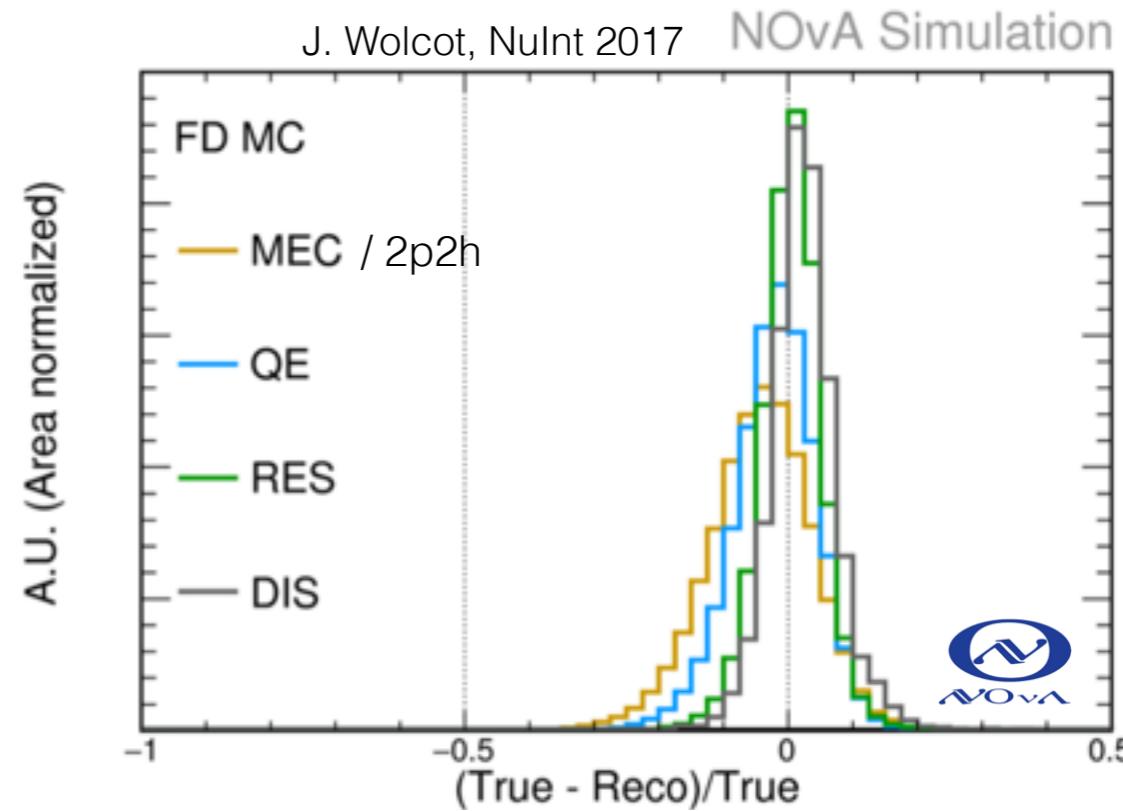
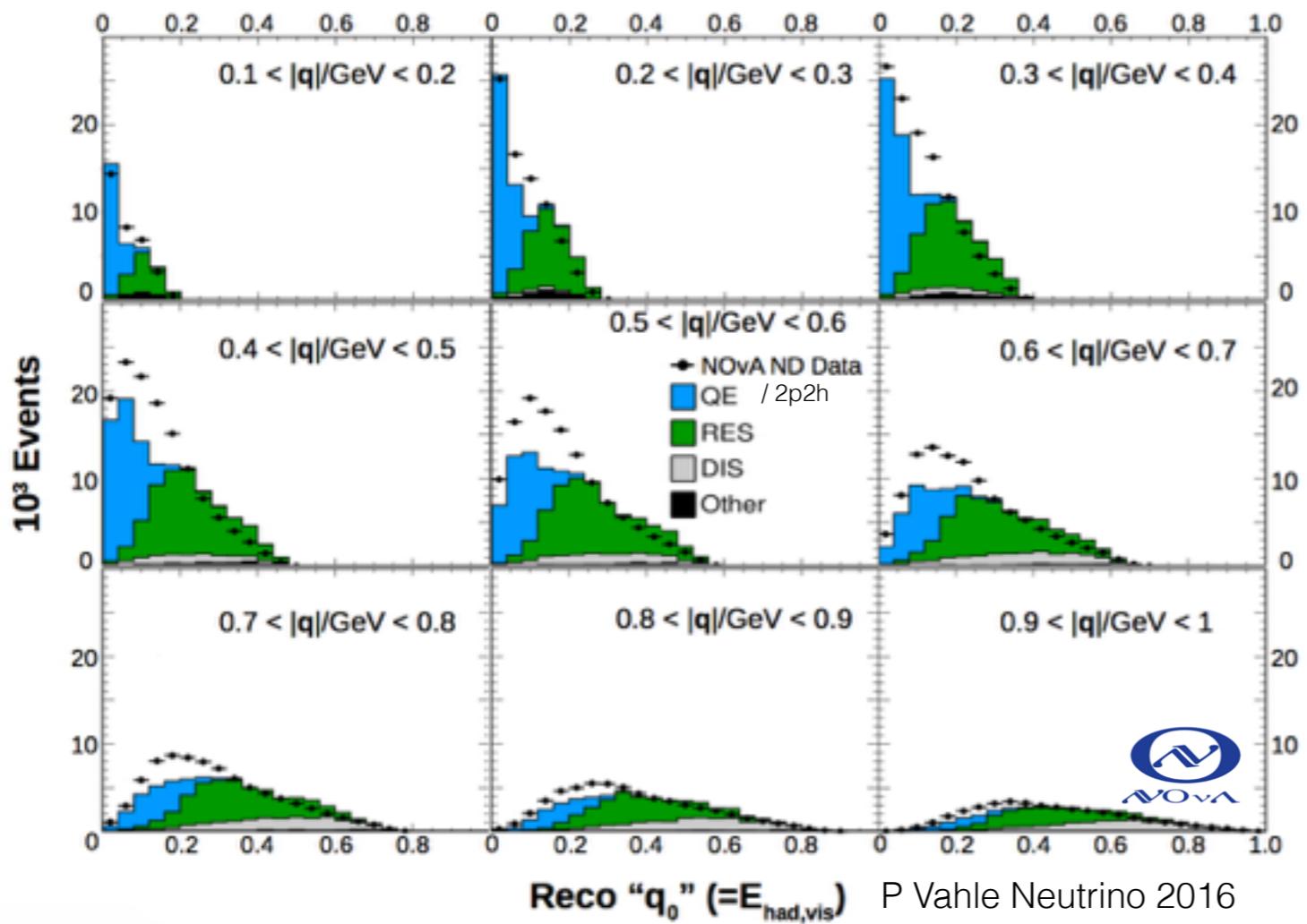
# NOvA Cross-section Model

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Use GENIE MC generator and uncertainties

## Some additions/modifications

- Empirical 2p2h model, tuned to match ND data
- Parameters to cover RPA uncertainties
- Alternative tuning of CC1 $\pi$  model [Eur. Phys. J. C 76, 474 (2016)]





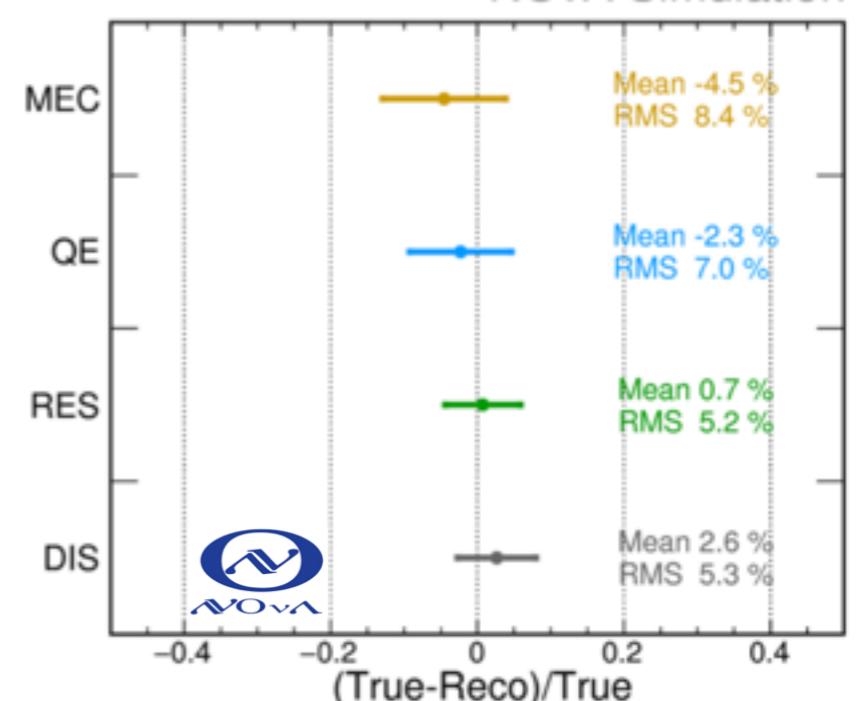
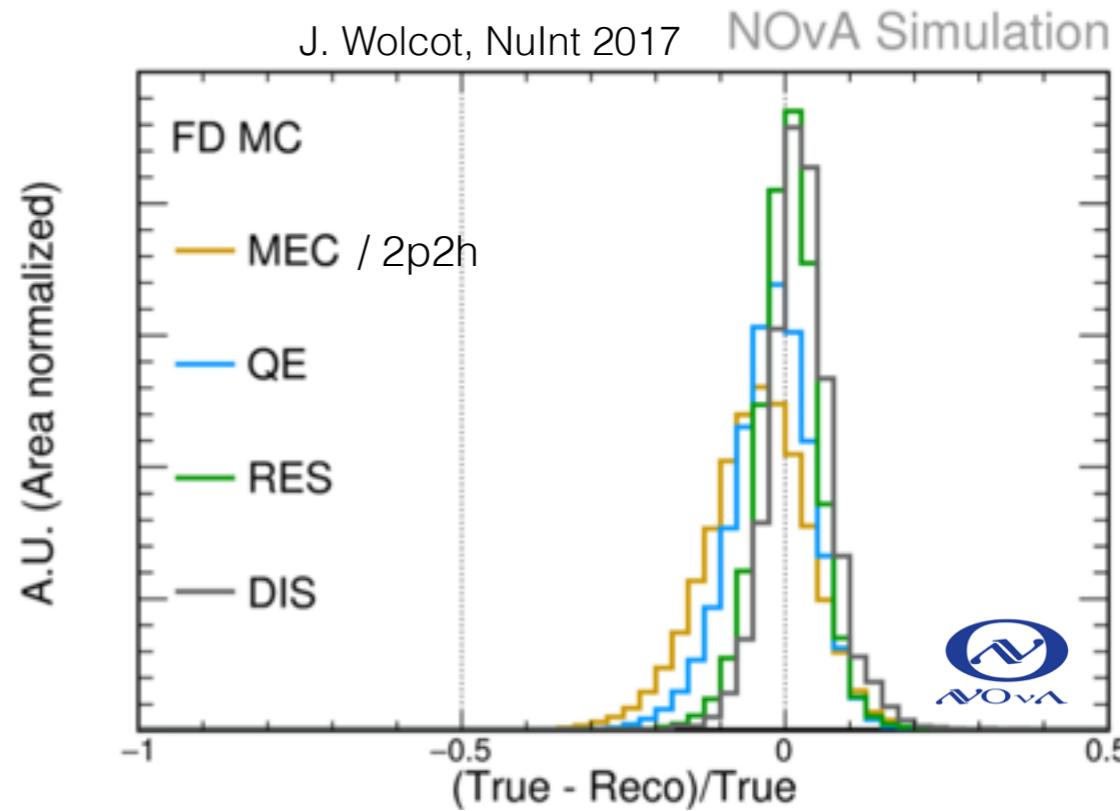
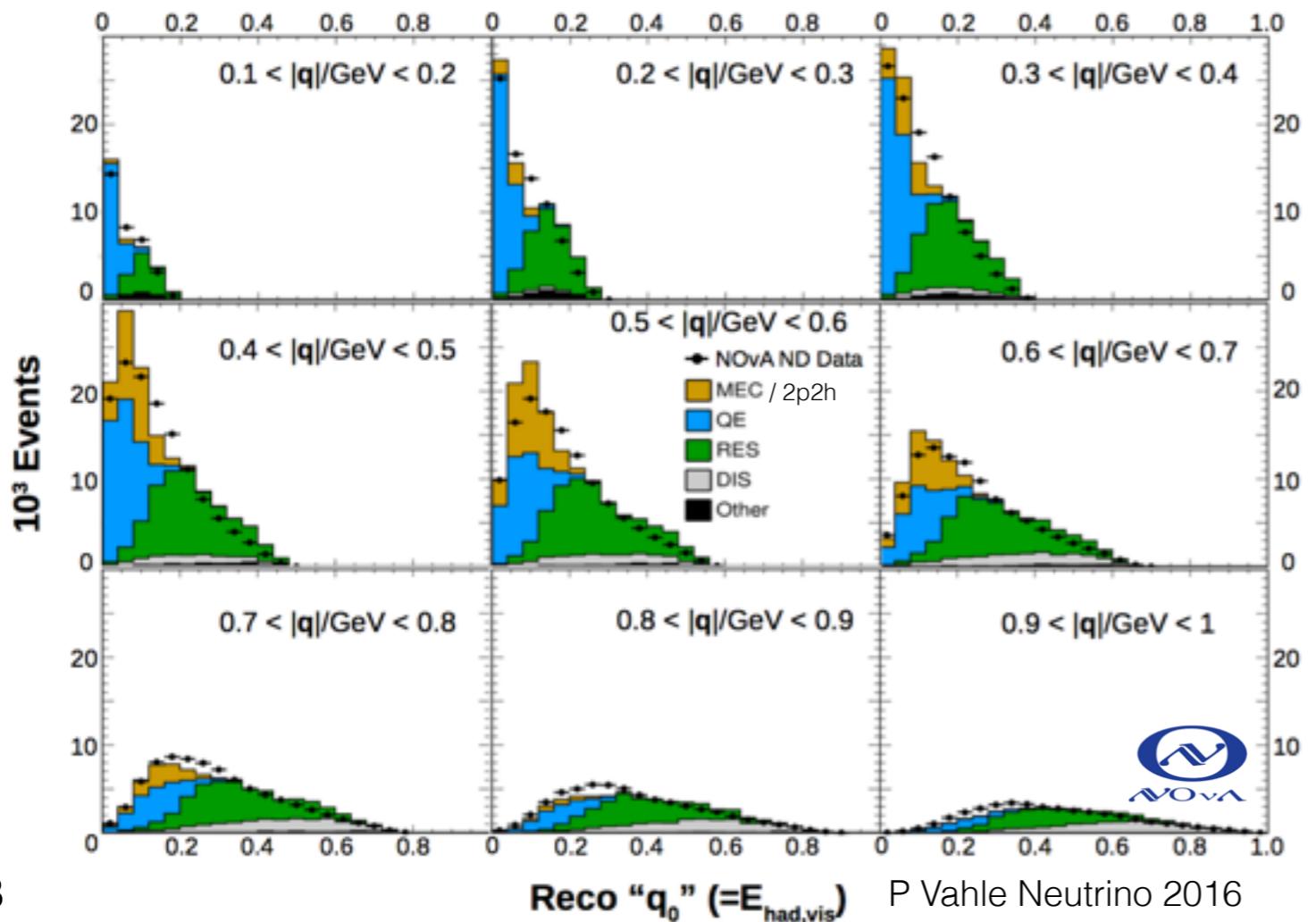
# NOvA Cross-section Model

WARWICK  
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Use GENIE MC generator and uncertainties

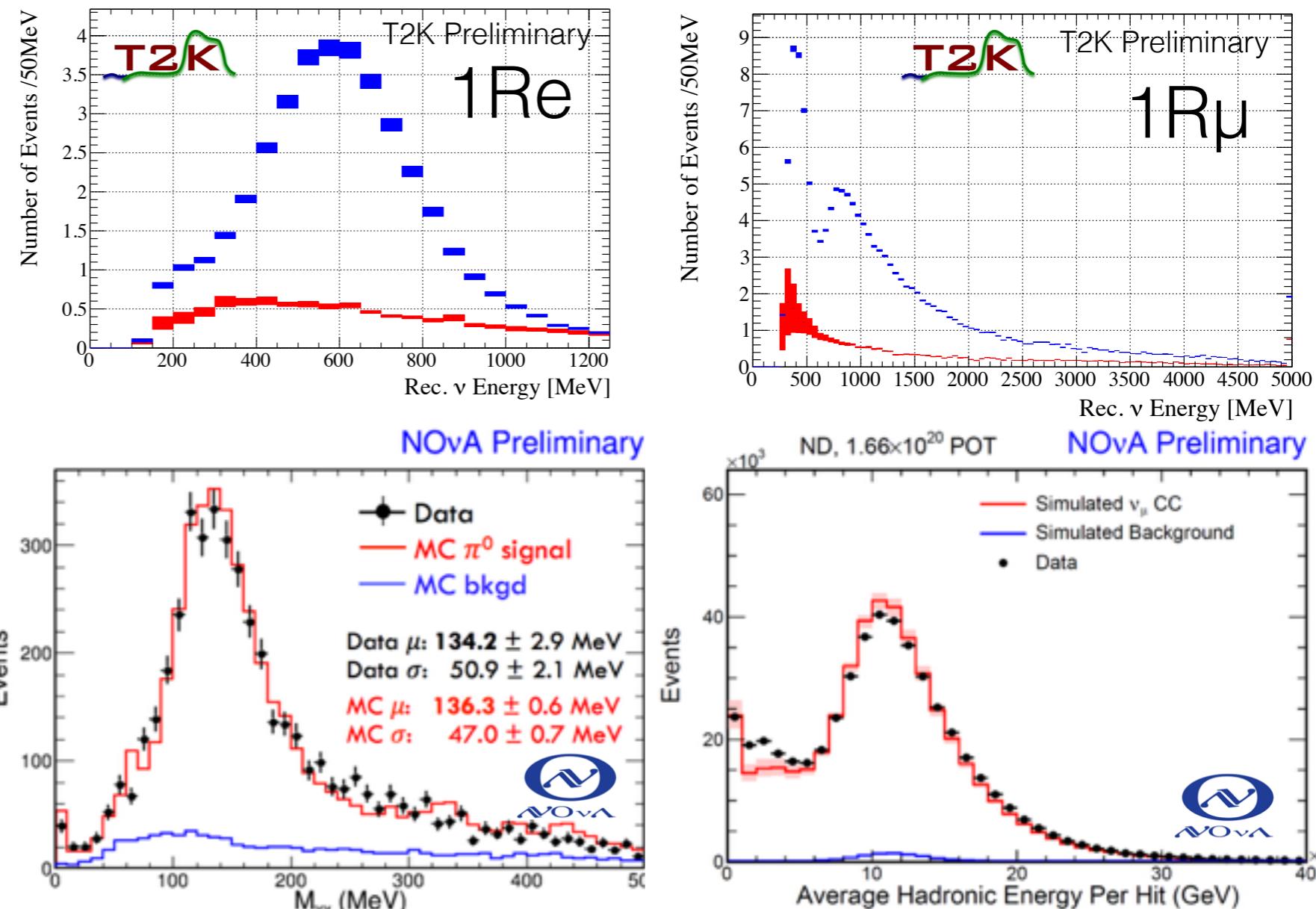
## Some additions/modifications

- Empirical 2p2h model, tuned to match ND data
- Parameters to cover RPA uncertainties
- Alternative tuning of CC1 $\pi$  model [Eur. Phys. J. C 76, 474 (2016)]



# Detector Modelling Uncertainties

SK detector response evaluated with atmospheric sample



Detector modelling uncertainties typically from data MC comparisons in control samples  
May be limited by control sample statistics

# T2K Systematic Uncertainties

ND280 constraint

13% → 3%

Pion Final State  
Interactions (FSI) and  
Secondary Interactions  
(SI) modelling important

Theoretical uncertainty  
 $v_e$  to  $v_\mu$   
Difficult to constrain with  
near detector

Error Source	$\mu$ sample [%]		$e$ sample [%]	
	$v$	$\bar{v}$	$v$	$\bar{v}$
SK Detector	1.9	1.6	3.0	4.2
SK FSI+SI+PN	2.2	2.0	2.9	2.5
ND280 Constraint (Flux + Cross Section)	3.3	2.7	3.2	2.9
$\sigma(v_e)/\sigma(v_\mu)$	-	-	2.6	1.5
NC 1γ	-	-	1.1	2.6
NC other	0.3	0.1	0.1	0.3
Total Systematic	4.4	3.8	6.3	6.4
Statistical	6.5	12	12	40

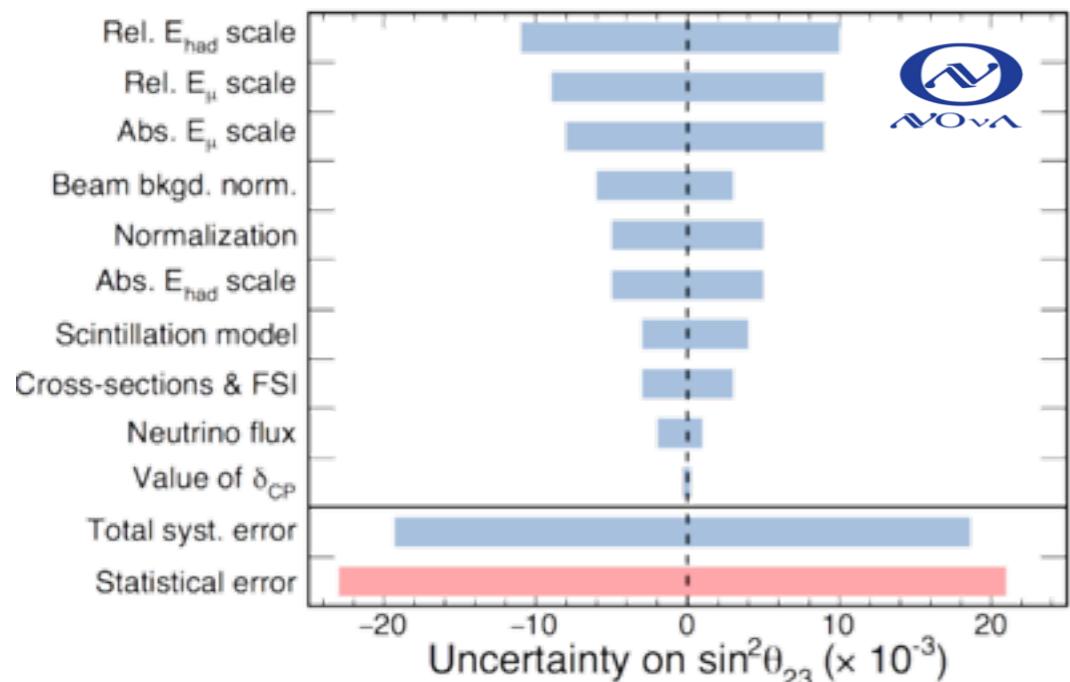
T2K preliminary (final systematics pending)

Total systematic uncertainty  
~4 - 6%

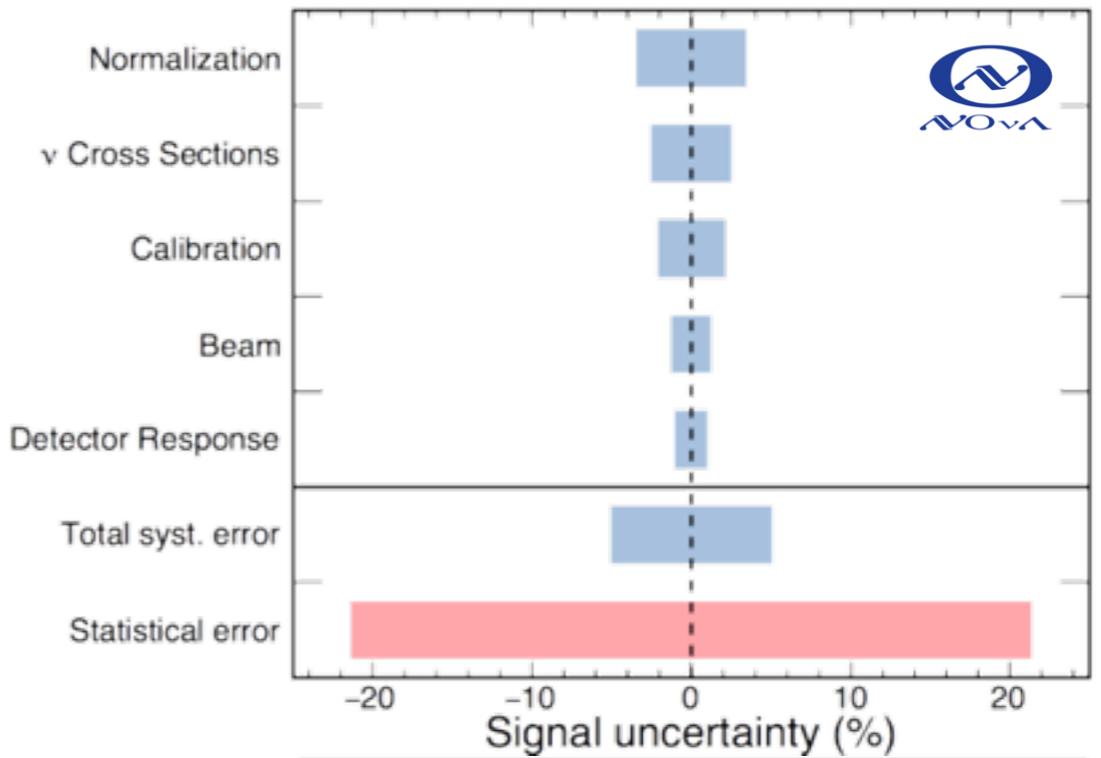
Smaller than stats. uncertainty  
(for now!)

# NOvA Systematic Uncertainties

$v_\mu$



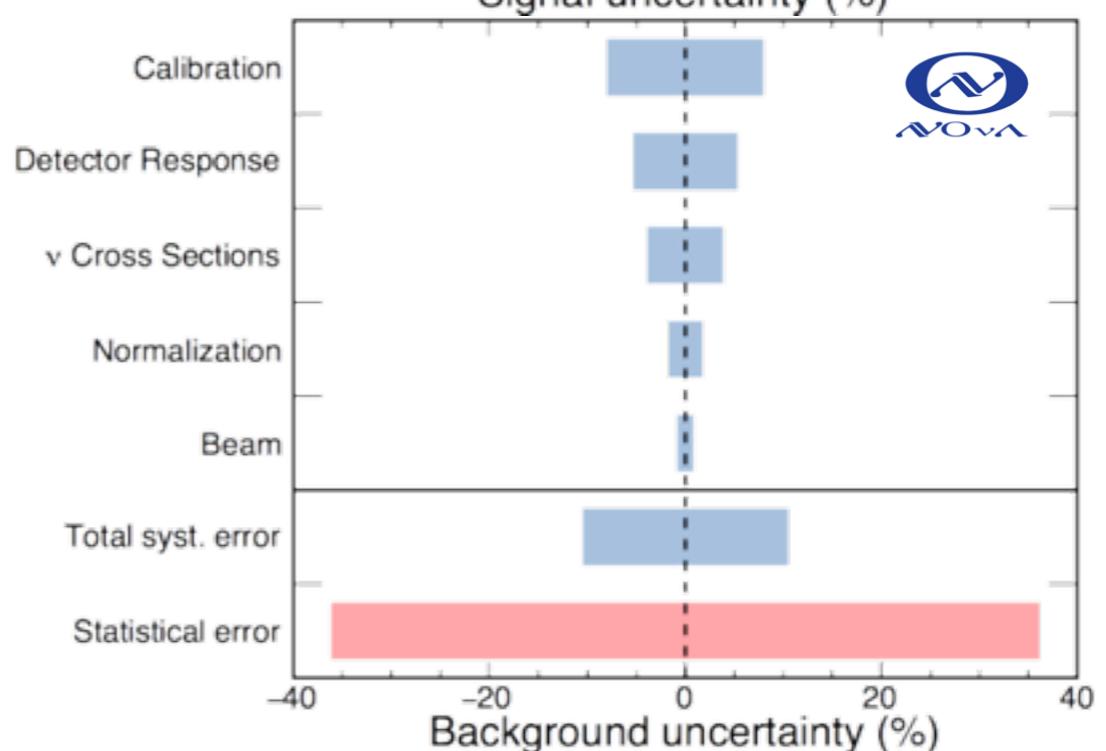
$v_e$



$v_e \sim 5\text{-}10\%$

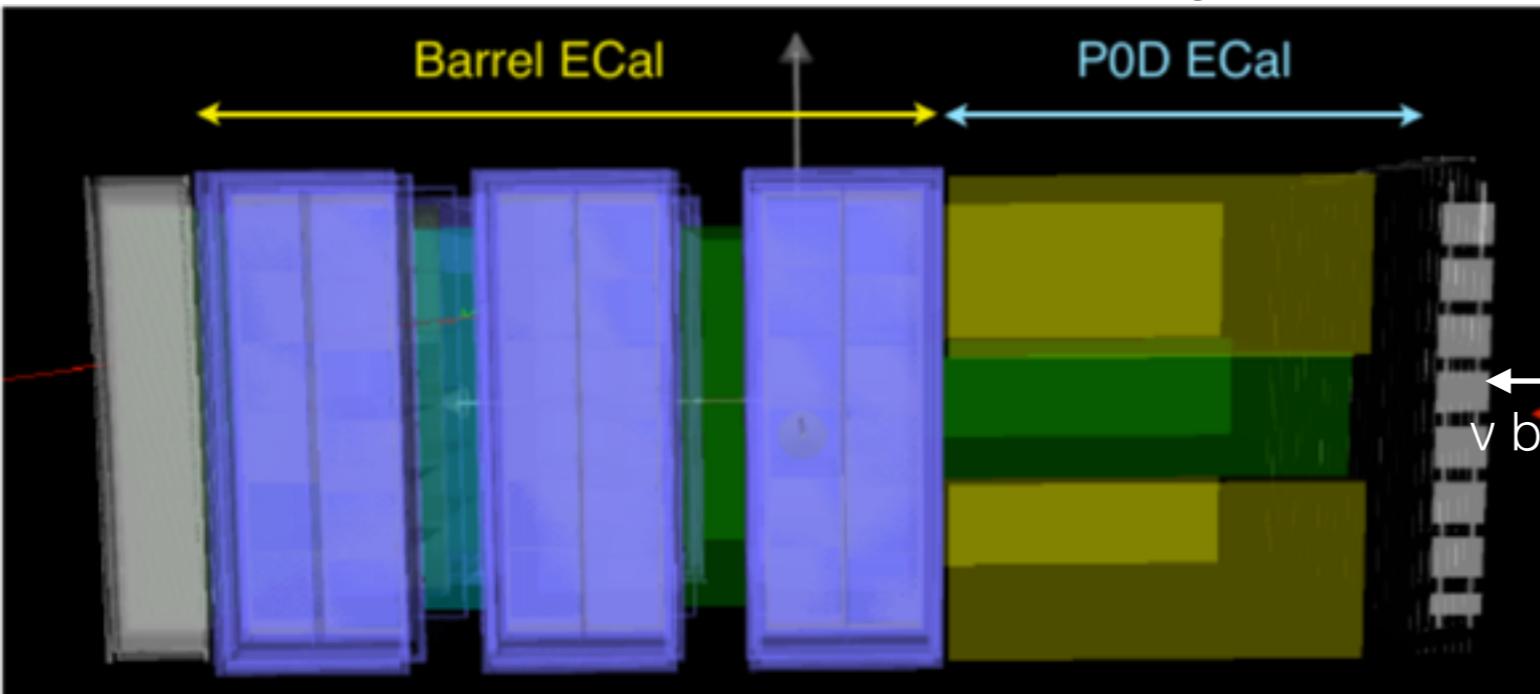
$v_\mu \sim 3\text{-}4\%$

Energy scale  
uncertainties dominate  $v_\mu$

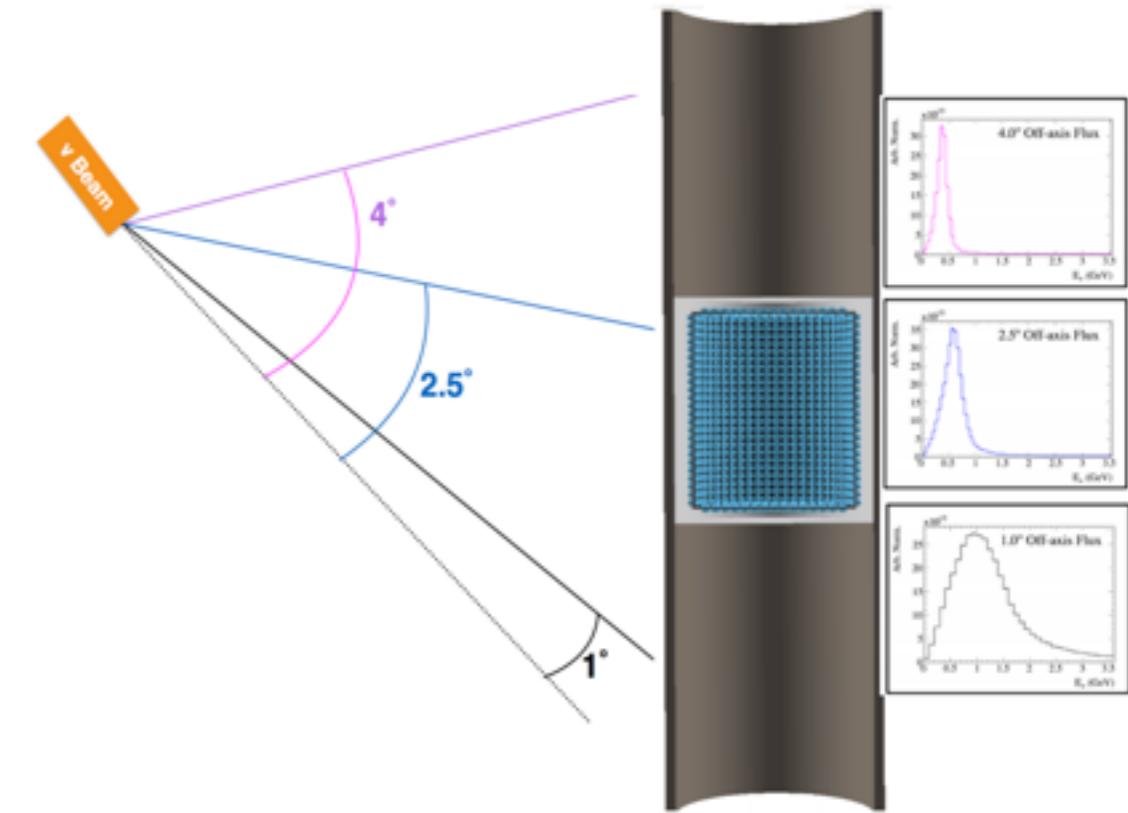


# Near Detector Development

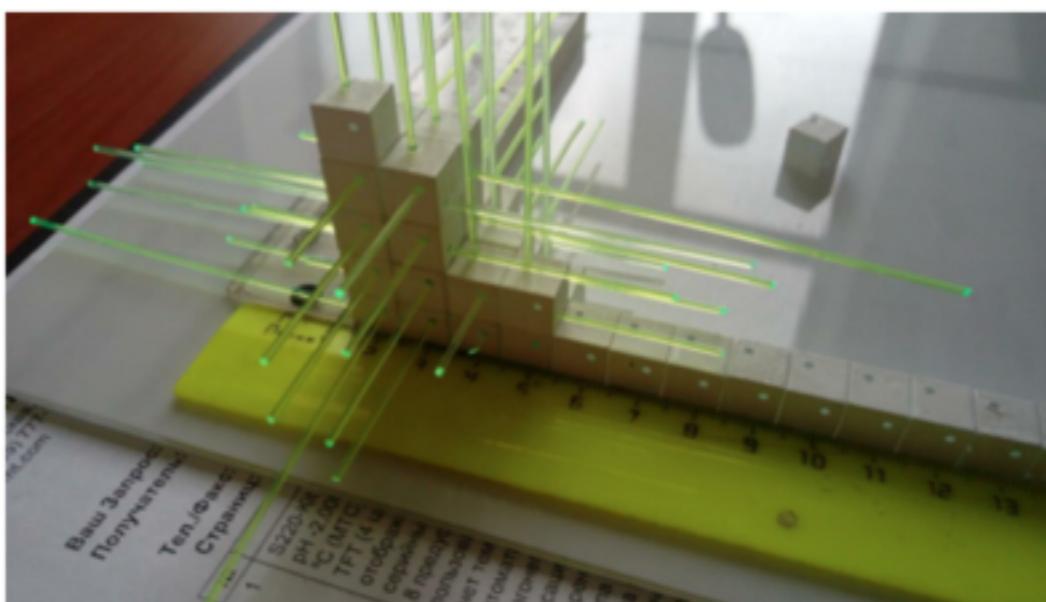
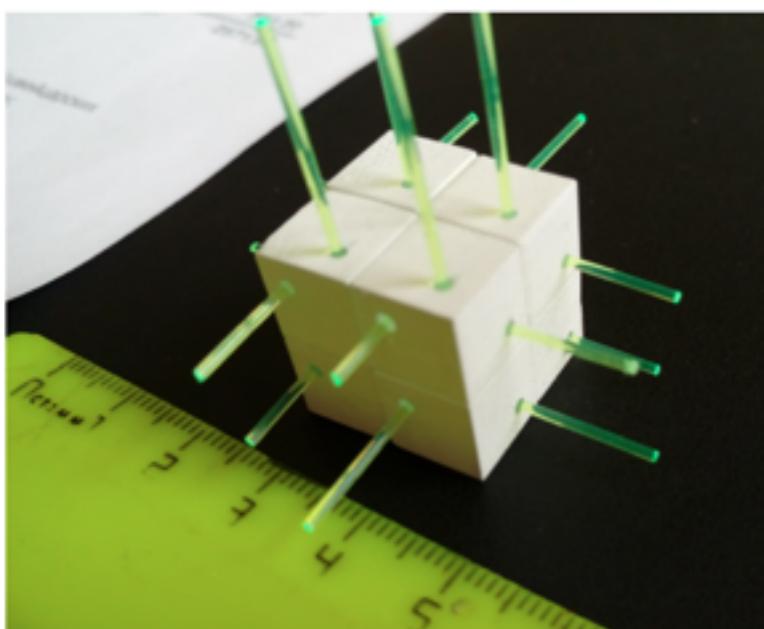
Planned ND280 Near Detector Upgrade



E61 Experiment

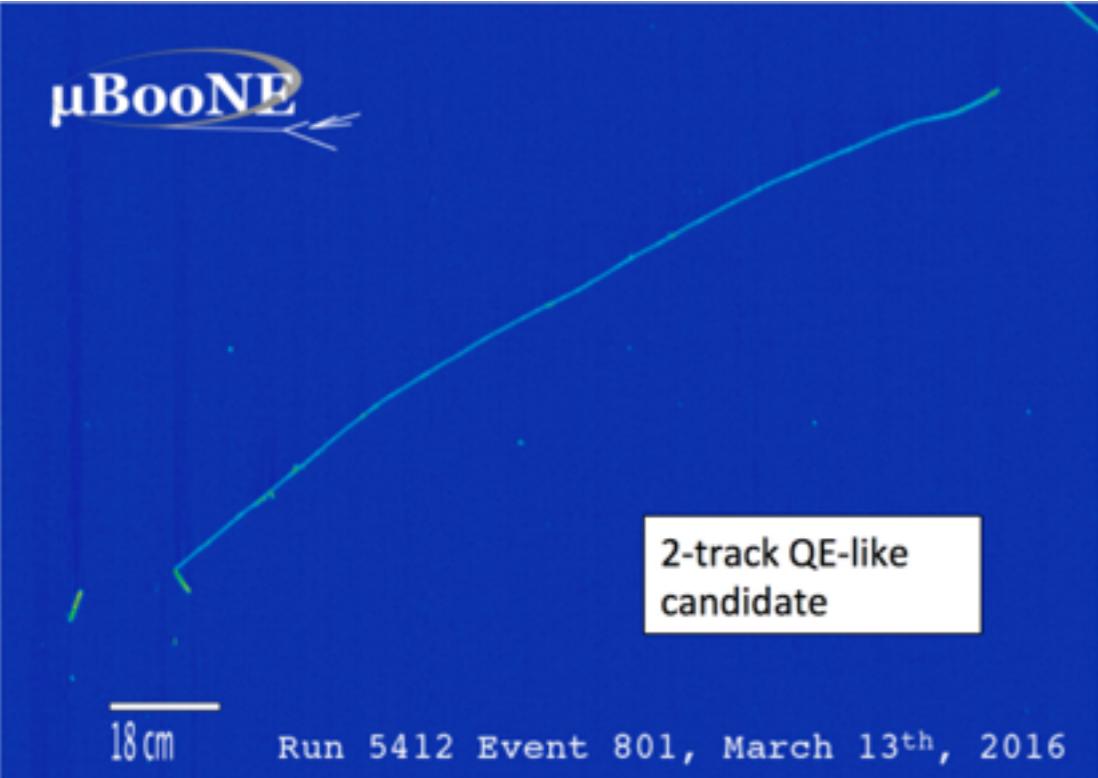


Near detector upgrades for T2K-II and T2HK era  
New target with increased angular acceptance



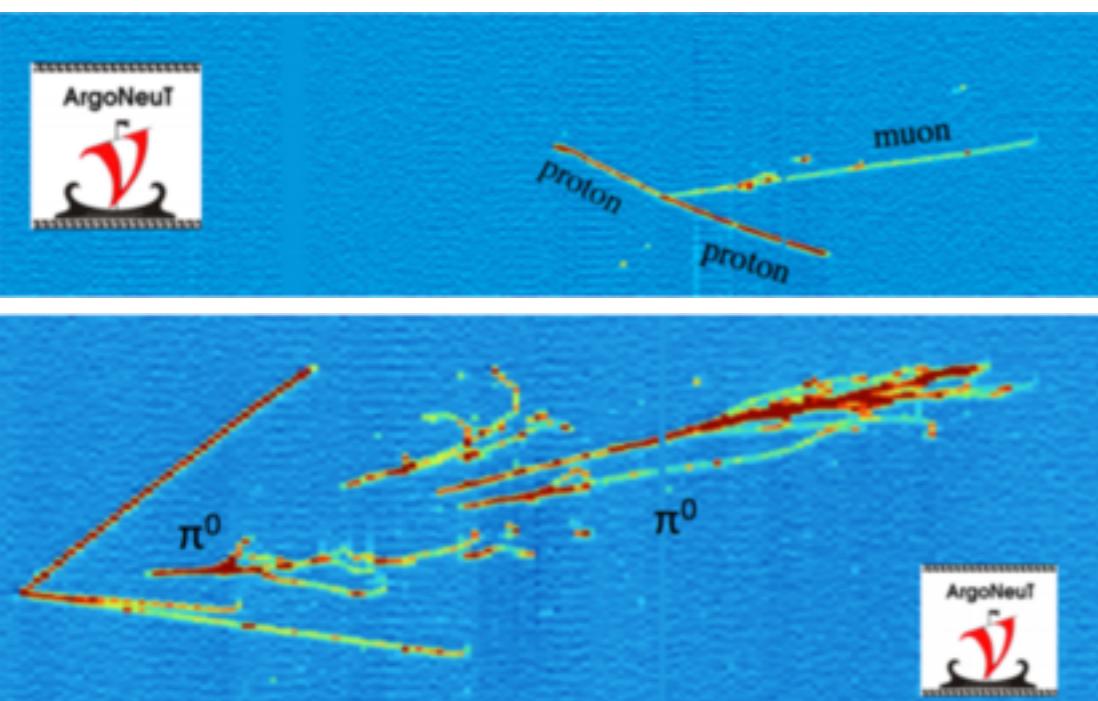
Intermediate Water-Cherenkov detector  
Map detector response using multiple off-axis angles

# Near Detector Development

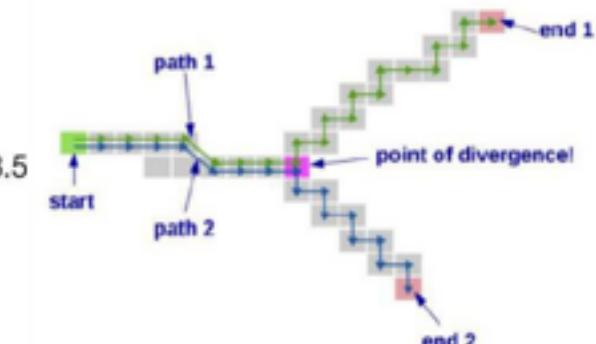
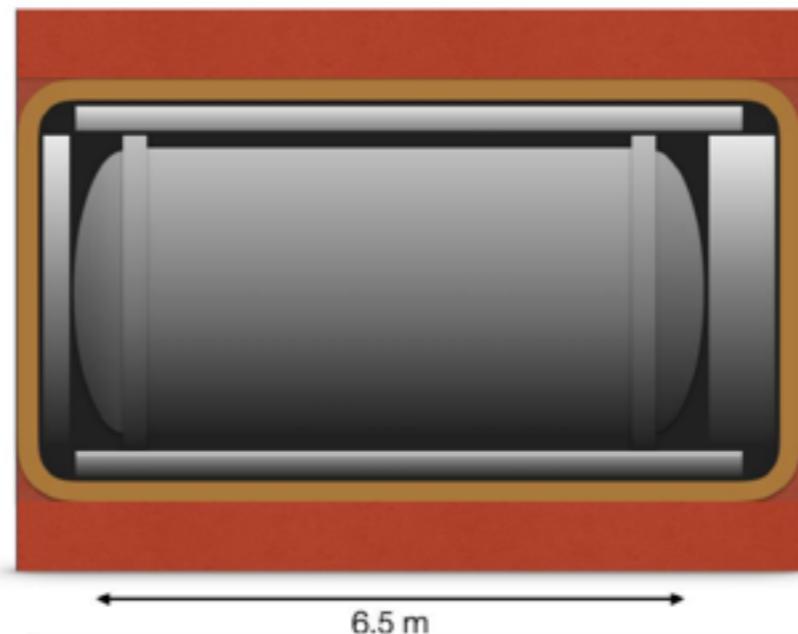


Several Argon TPC experiments  
Natural ND candidates for DUNE

Precisely image the neutrino interaction vertex  
(better constraints on neutrino-nucleus  
interaction models → better energy  
measurement)



DUNE High Pressure Gaseous TPC ND



Ultra-low thresholds with gaseous TPC

# Summary



Statistical precision promised by future high beam power and high mass experiments place high demands on the systematic uncertainties that experiments must reach

T2K and NOvA have reported systematics uncertainties in the range  $\sim 3 - 10\%$  level

Reductions are needed today to make best use of the increasing statistical precision in the T2K and NOvA disappearance measurements

Improved flux determination,  $\nu$ -nucleus interaction modelling and understanding of detector response will all play a role



# Systematic Uncertainties in Long Baseline Neutrino Oscillation Measurements

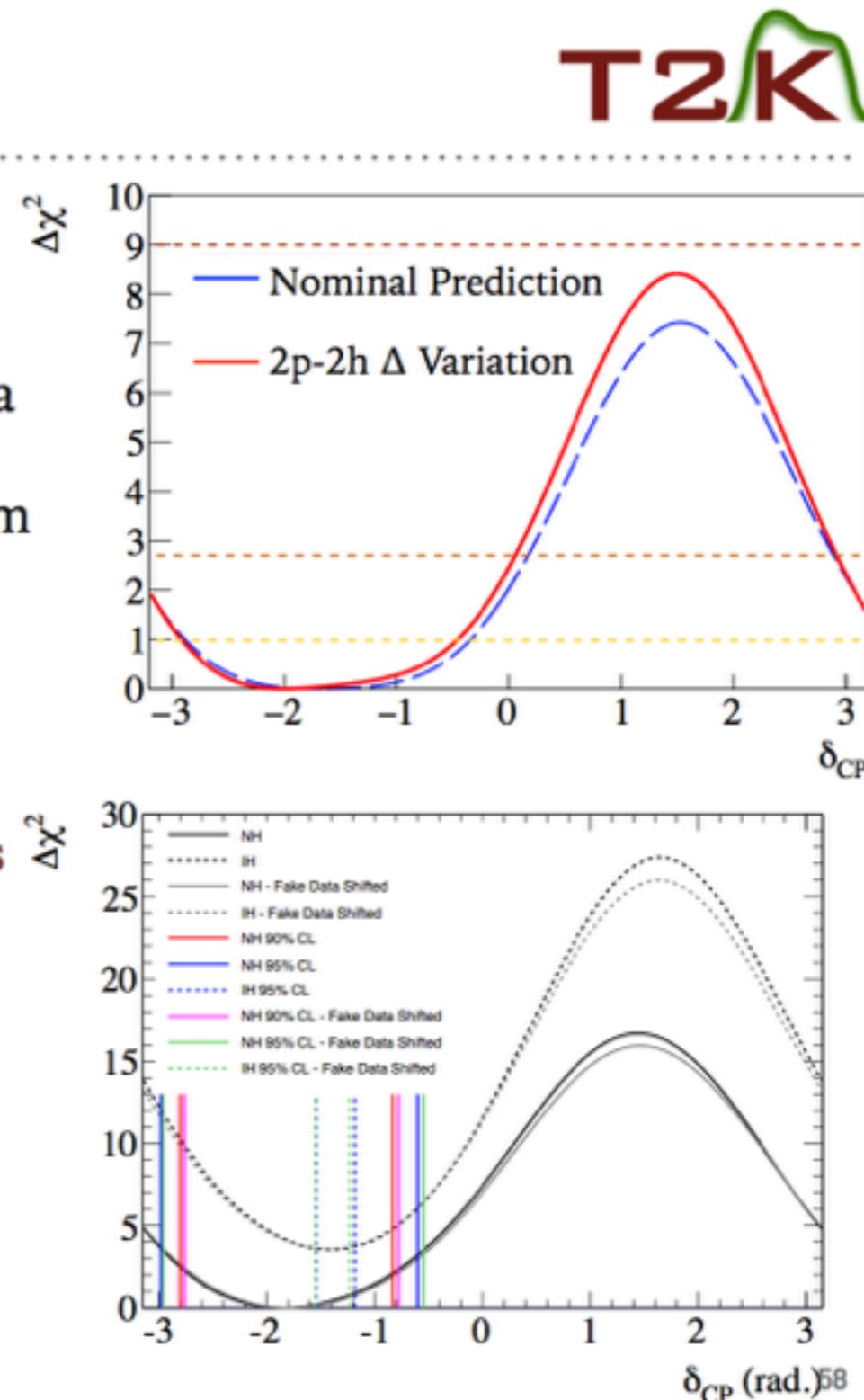


David Hadley  
21st December 2017  
Prospects in Neutrino Physics, NuPhys2017

# Fake Data Studies

## IMPACT ON CP PHASE

- ▶ Consider how changes to the  $\Delta\chi^2$  impact intervals calculated from data
  - ▶ Shift  $\Delta\chi^2$  observed in data (bottom plot) by difference observed in systematic study (top plot)
- ▶ Maximum shift in the NH  $2\sigma$  confidence interval mid-point was 1.7%
- ▶ Maximum change to the NH  $2\sigma$  confidence interval was 2.3%
- ▶ Impact on  $\delta_{cp}$  intervals is small

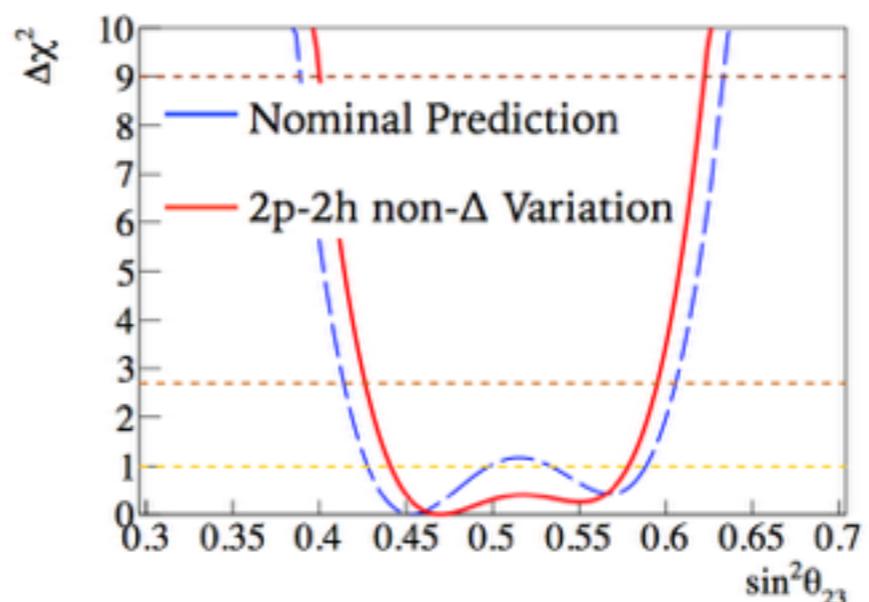
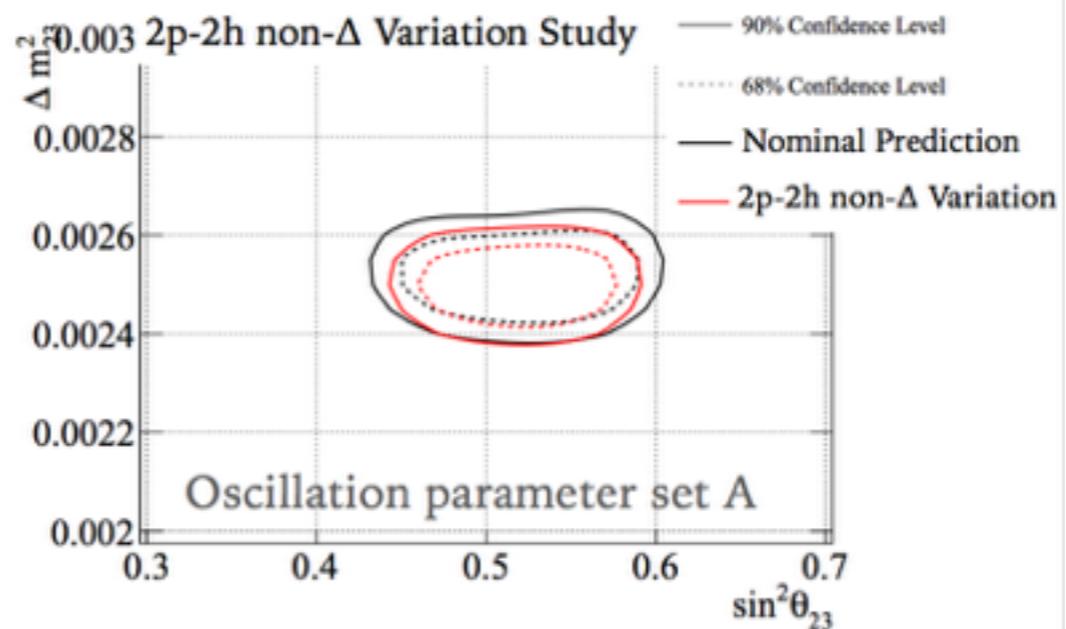


# Fake Data Studies

## IMPACT ON ATMOSPHERIC PARAMETERS



- In this study,  $\Delta m^2_{32}$  is biased to lower values
- $\sin^2\theta_{23}$  is biased towards maximal disappearance
  - Leads to narrower contour than fit to nominal prediction
- Shift towards maximal also seen in 1-D contour for oscillation parameter set B (bottom)



# Fake Data Studies

## ND280 DATA-DRIVEN VARIATION

- Take excess of data over prediction prior to ND280 fitting

- Assign excess to 1 of 3 types of interactions:

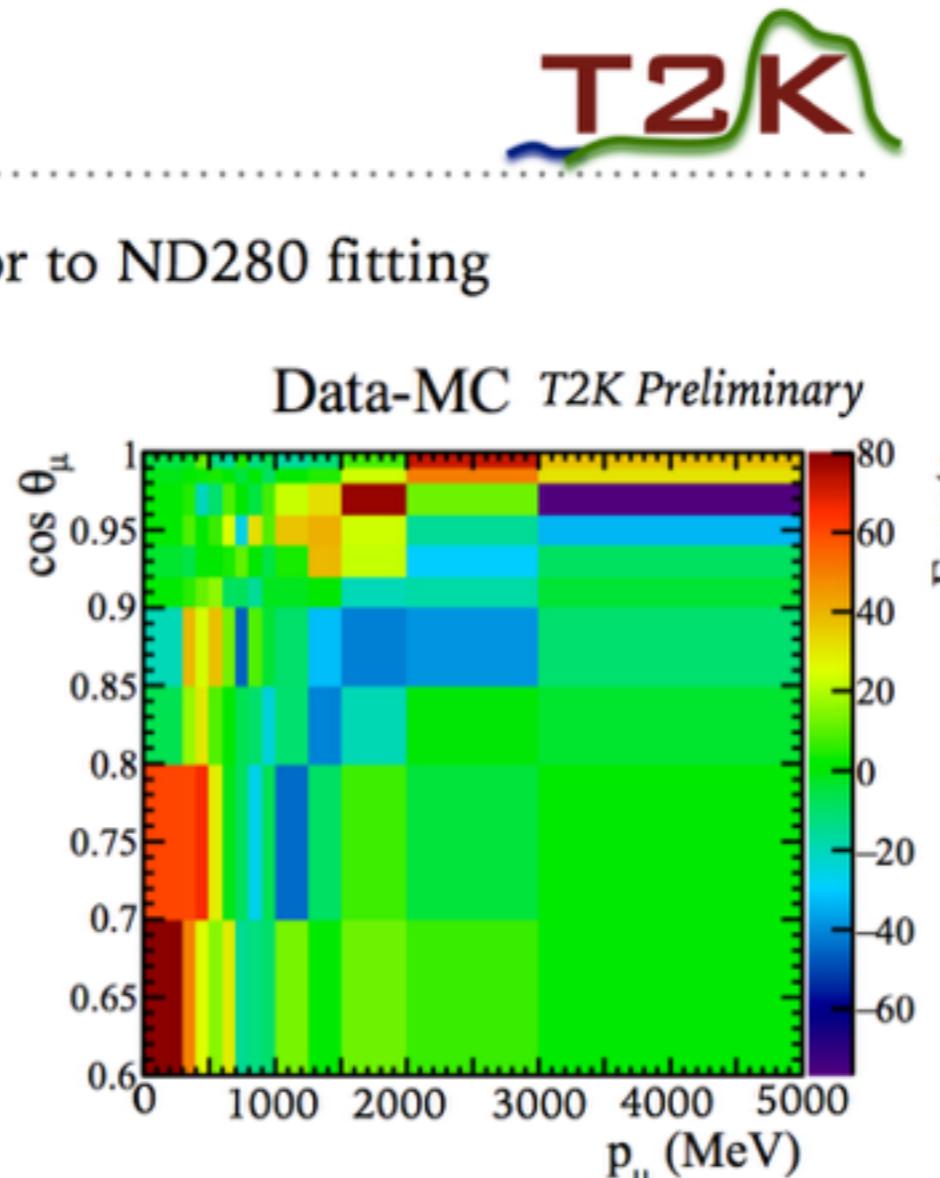
- CCQE
- 2p-2h  $\Delta$ -enhanced
- 2p-2h non- $\Delta$ -enhanced

- Apply modeled excess to predict rates ND280 and SK

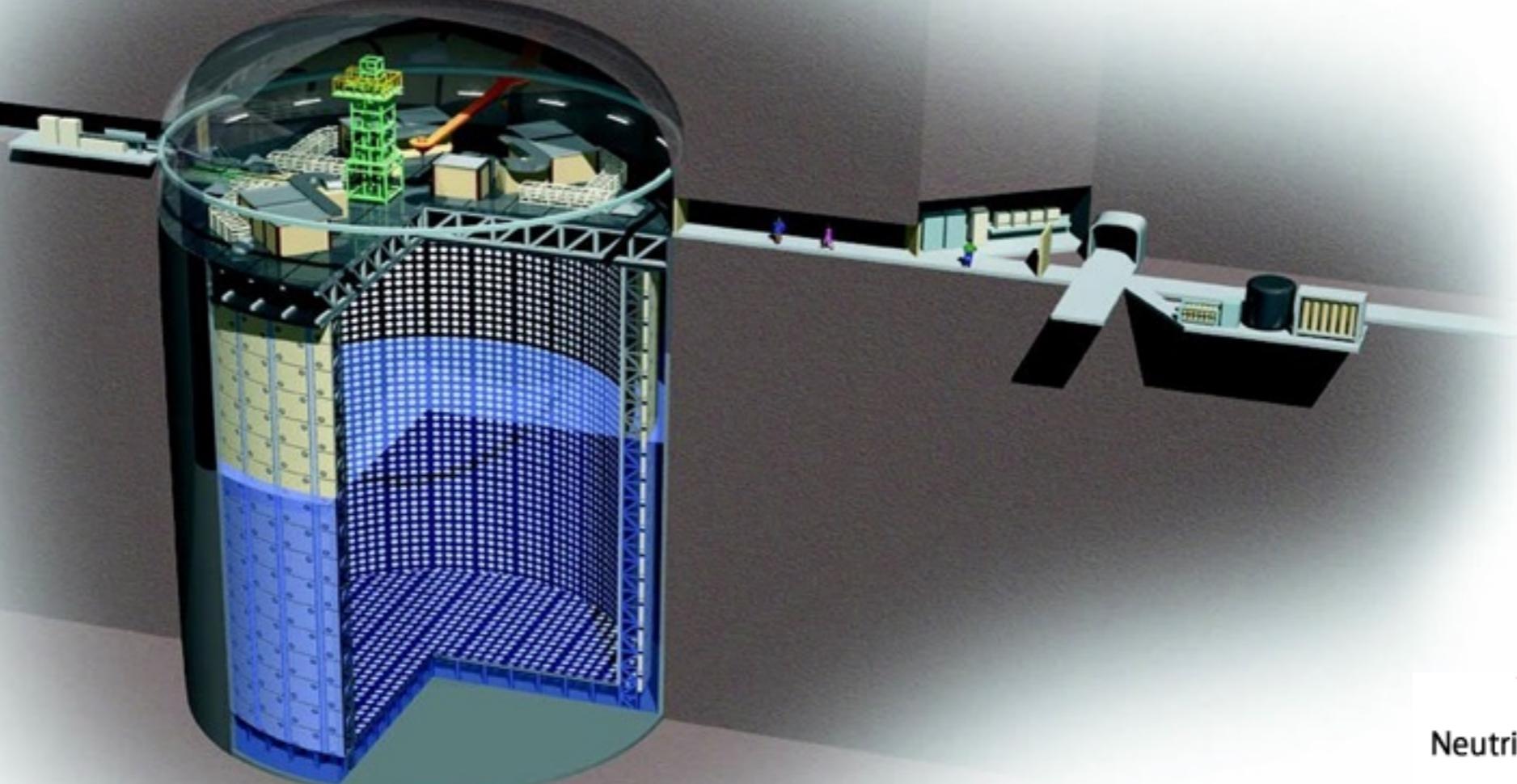
- Run fits

- Effect seen on  $\sin^2\theta_{23}$  and  $\Delta m^2_{32}$

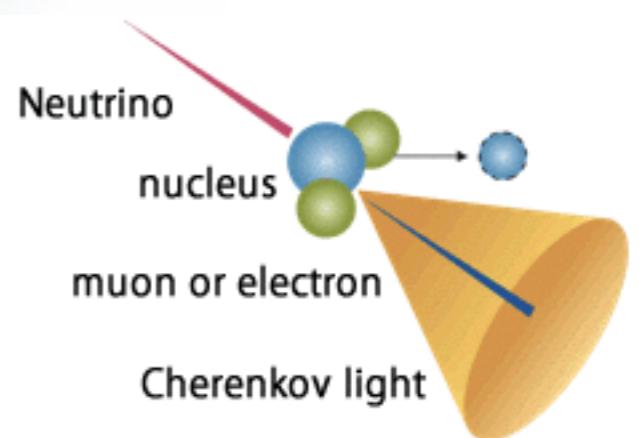
- No significant impact on the measured intervals for  $\delta_{cp}$



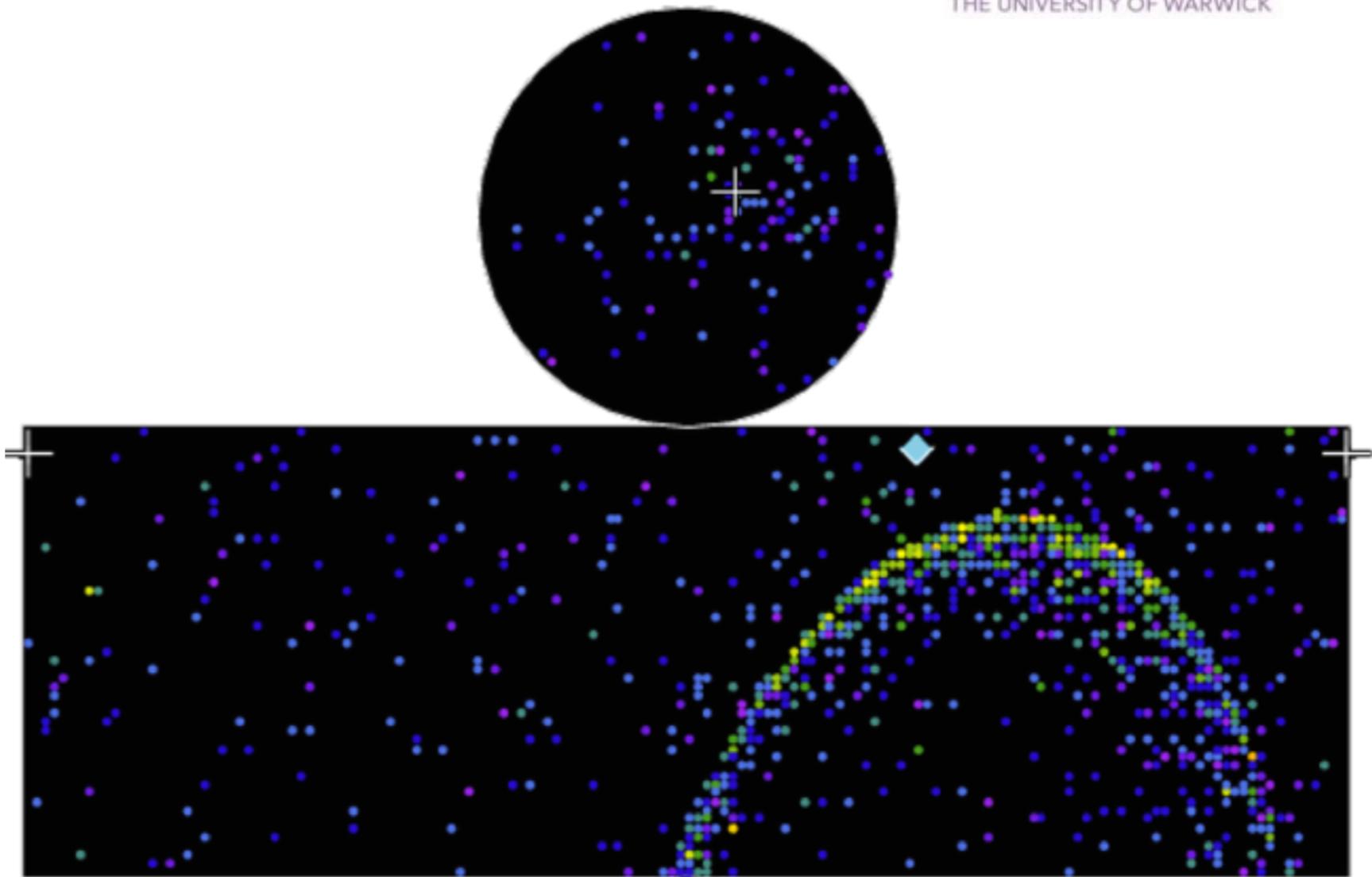
# Super-Kamiokande



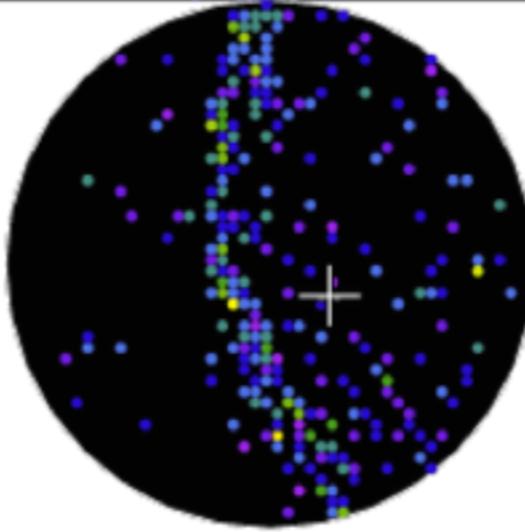
Water Cherenkov Detector  
>22.5 kt fiducial mass



# Water Cherenkov Technique

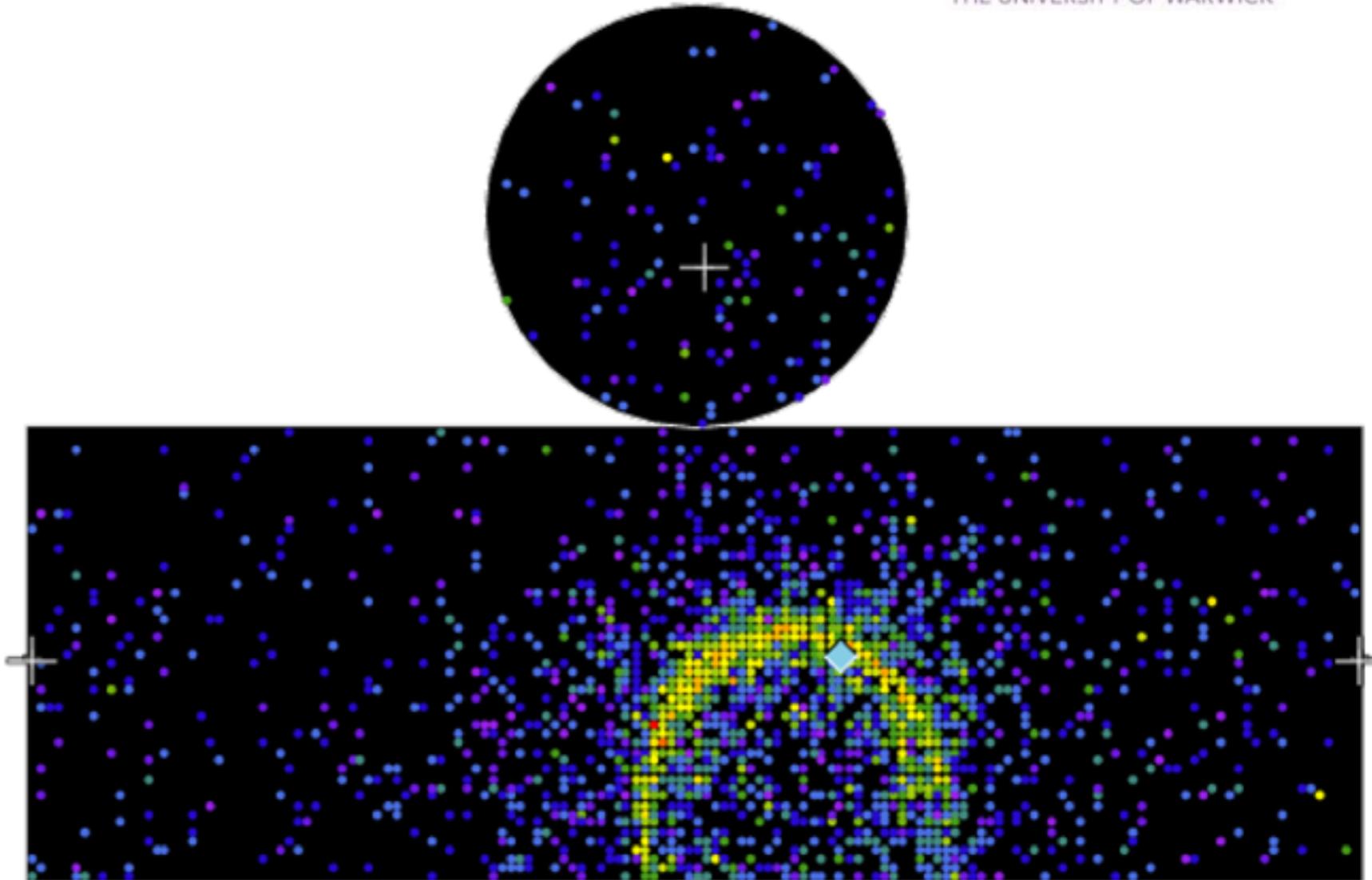
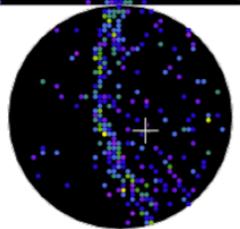
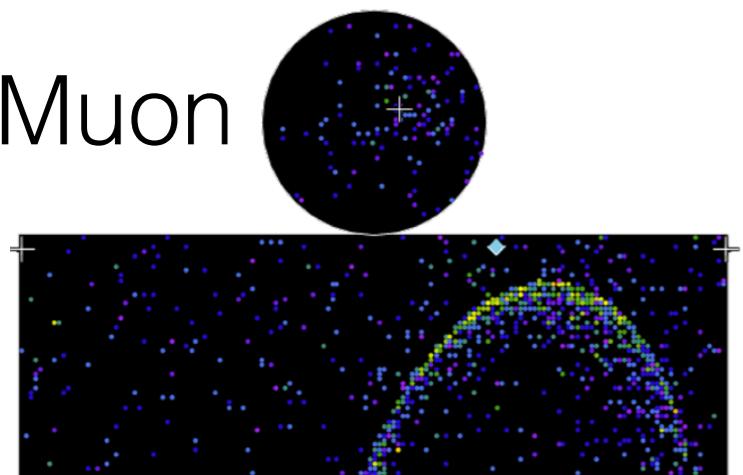


Muon

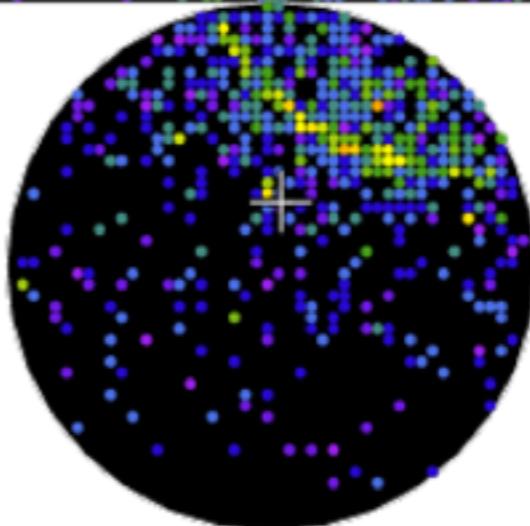


# Water Cherenkov Technique

Muon

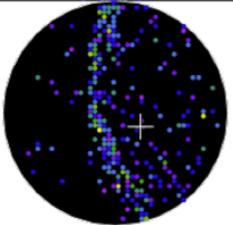
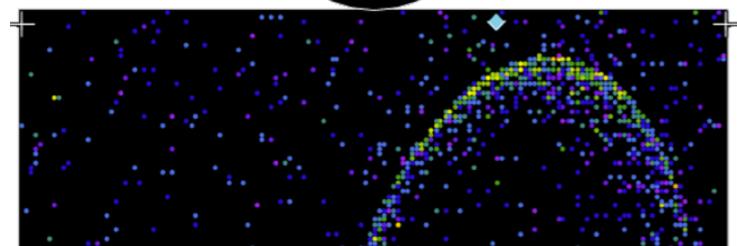
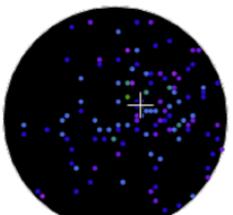


Electron

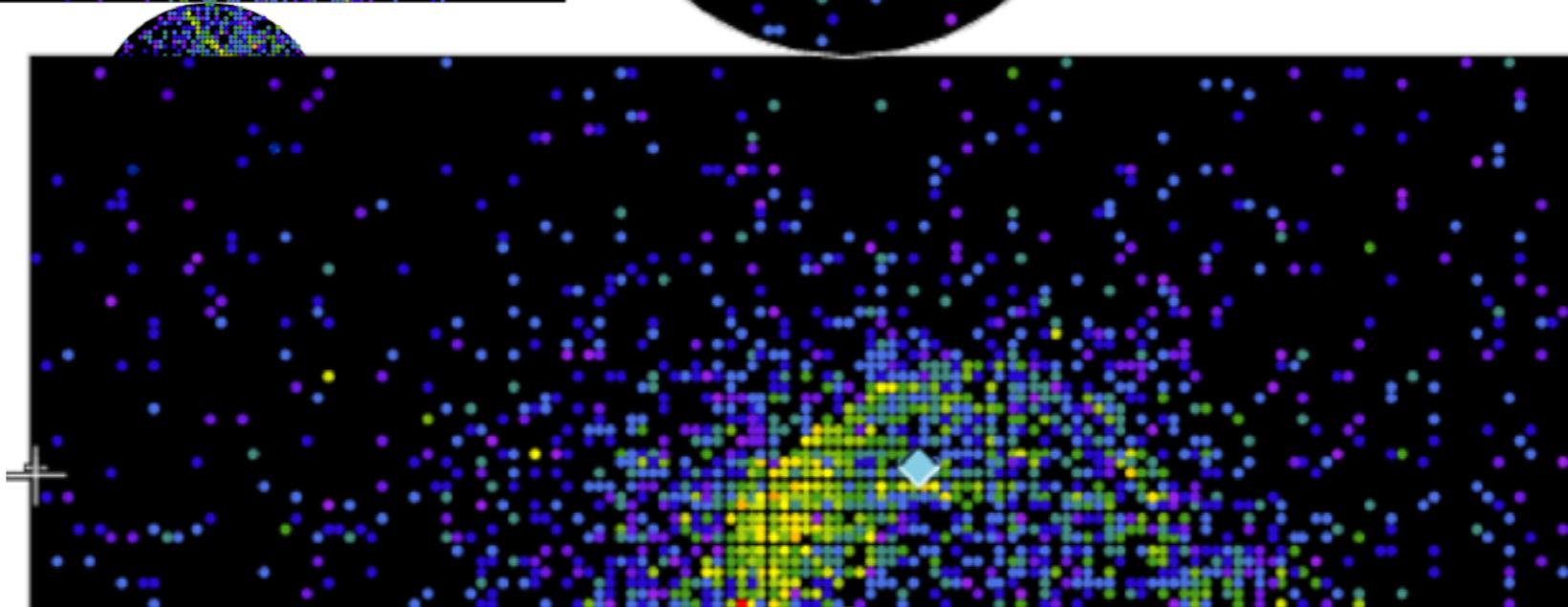
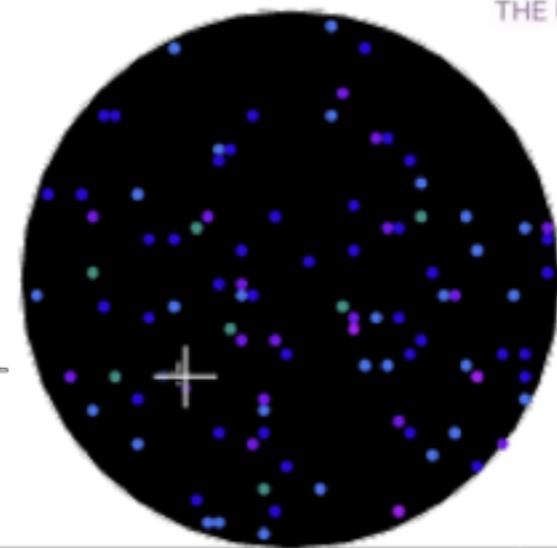
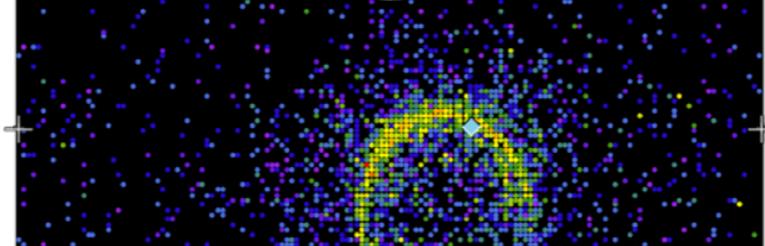
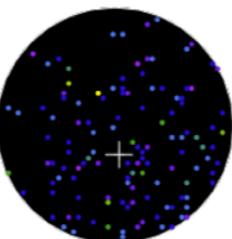


# Water Cherenkov Technique

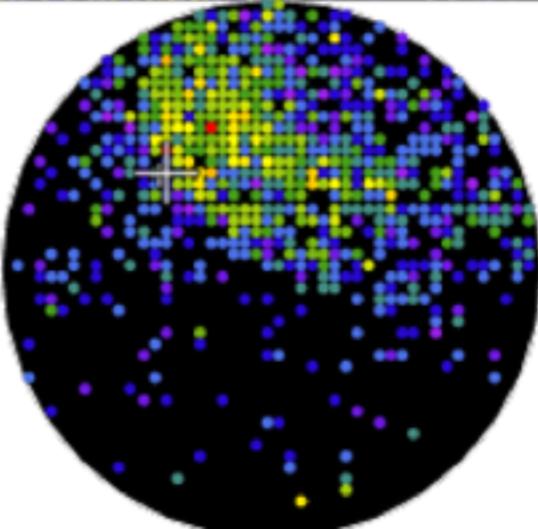
Muon



Electron

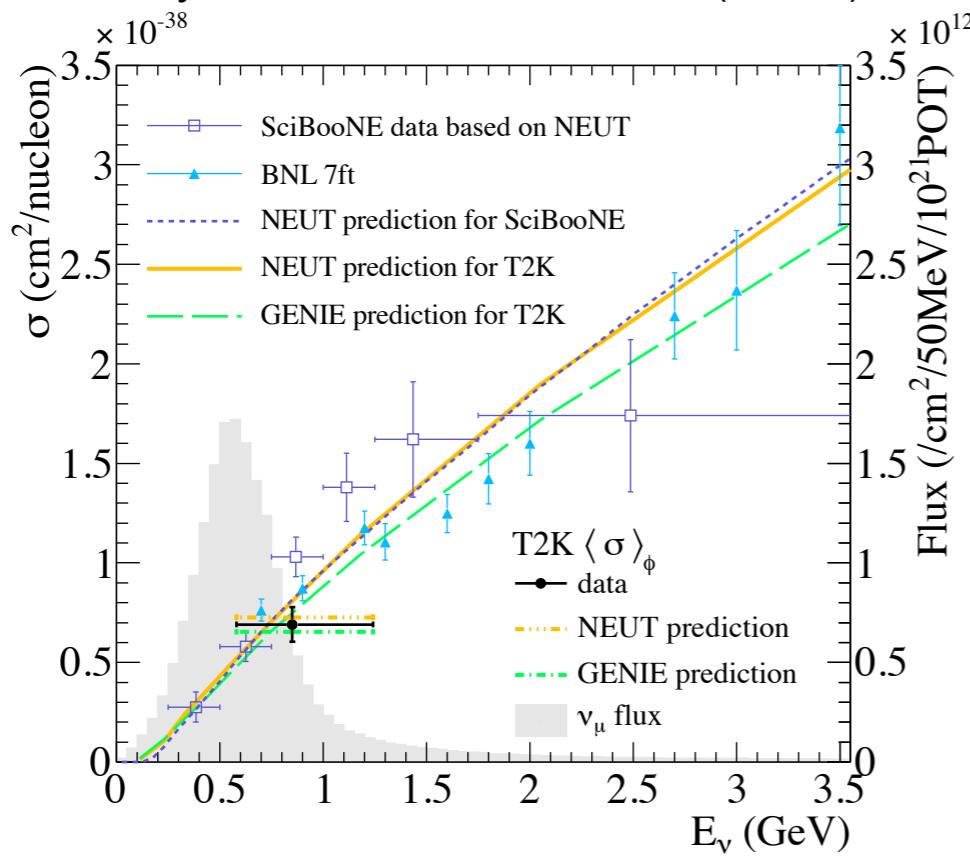


Neutral Pion

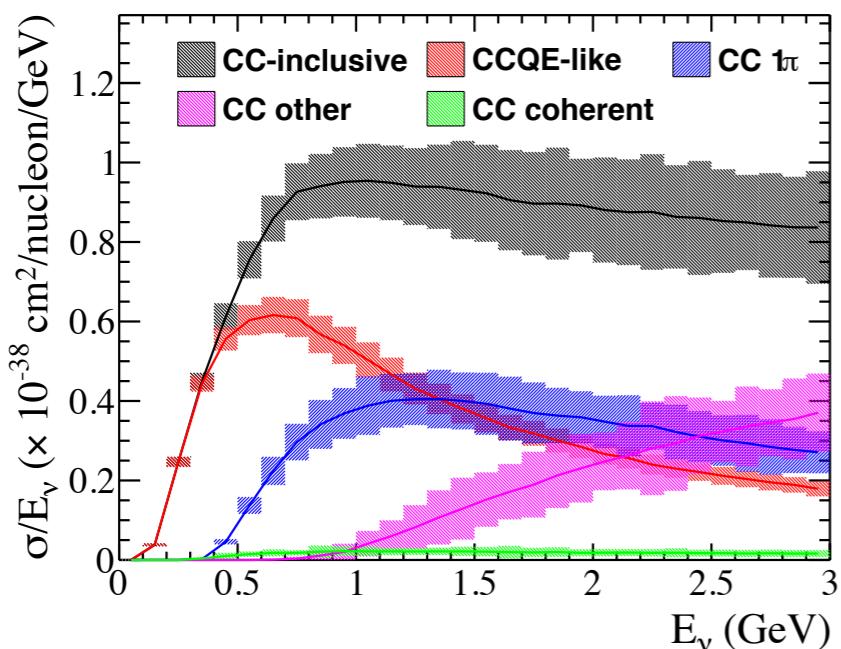
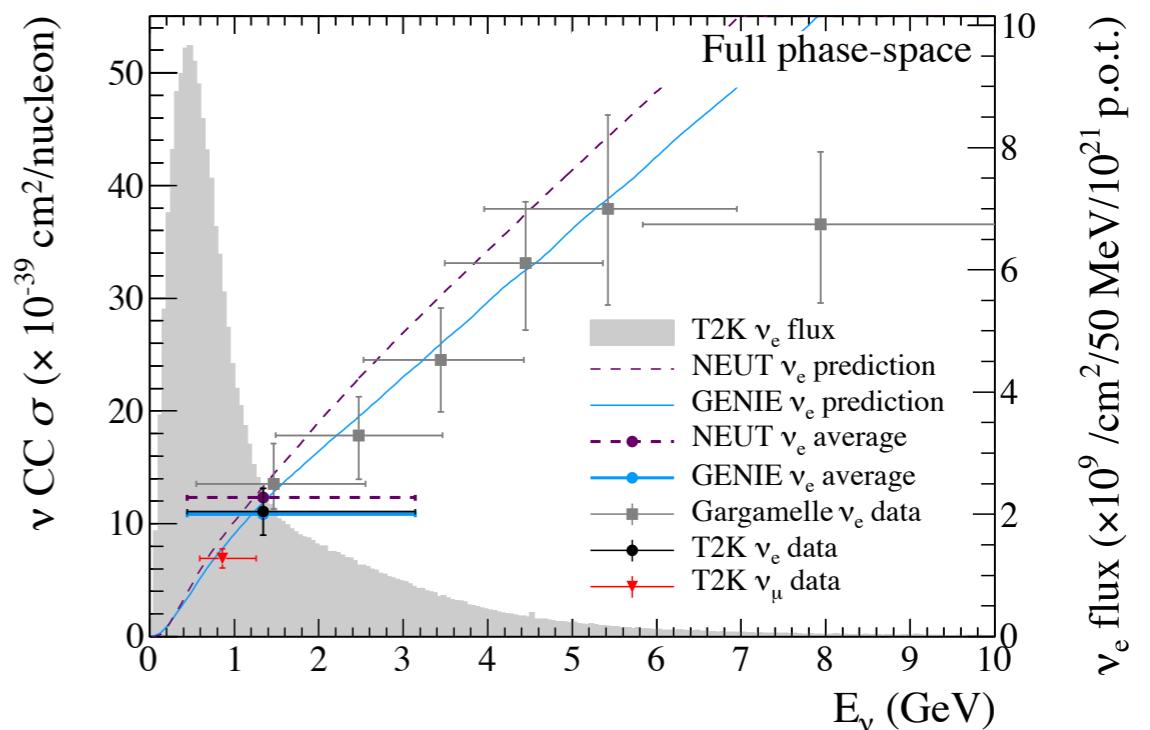


# ND280 Flux

Phys. Rev. D 87, 092003 (2013)



Phys. Rev. Lett. 113, 241803 (2014)



In neutrino-mode

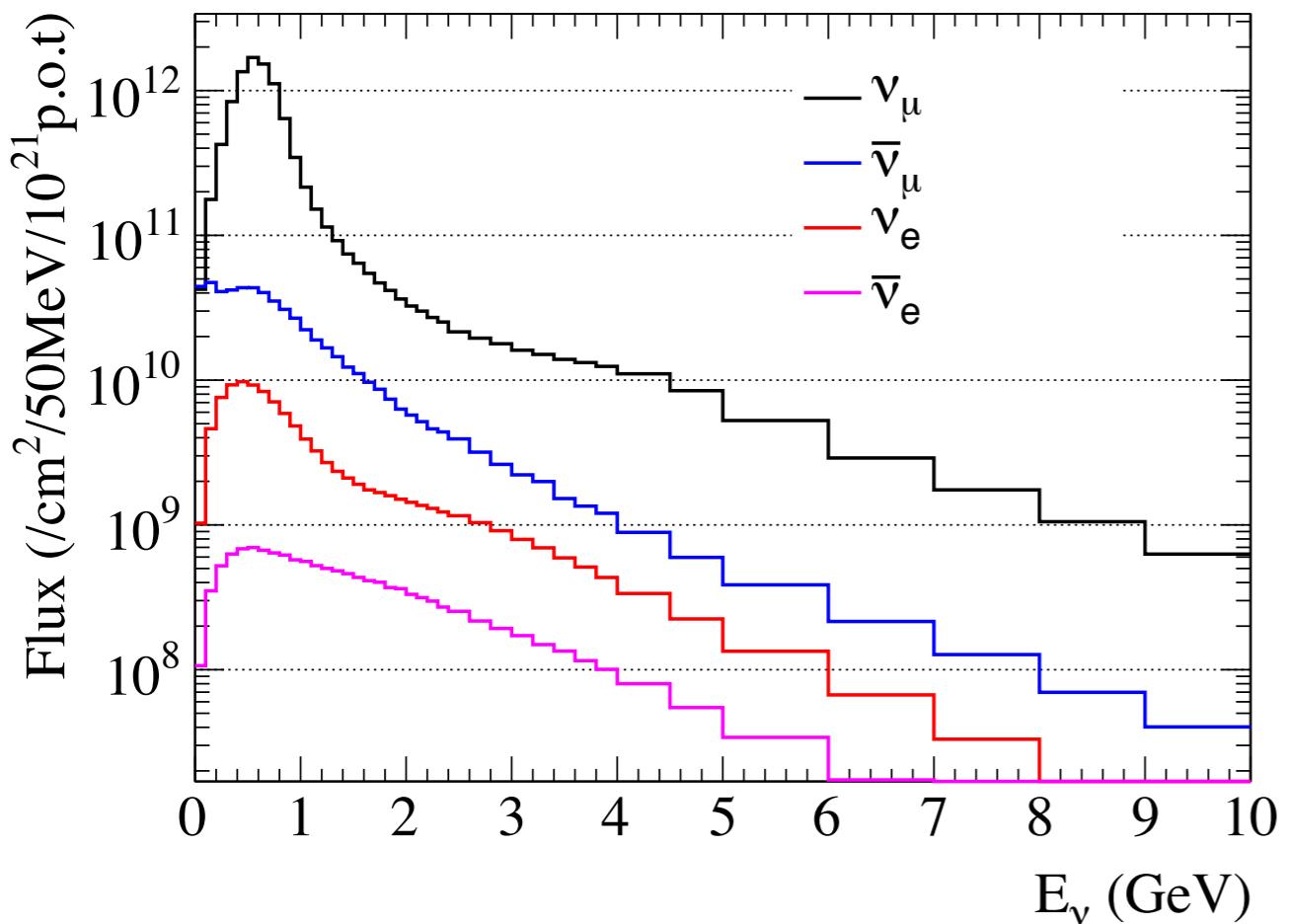
$\nu_\mu$  :  $\langle E \rangle = 0.85 \text{ GeV}, (\sim 90\%)$

$\nu_e$  :  $\langle E \rangle = 1.3 \text{ GeV}, (\sim 1\%)$

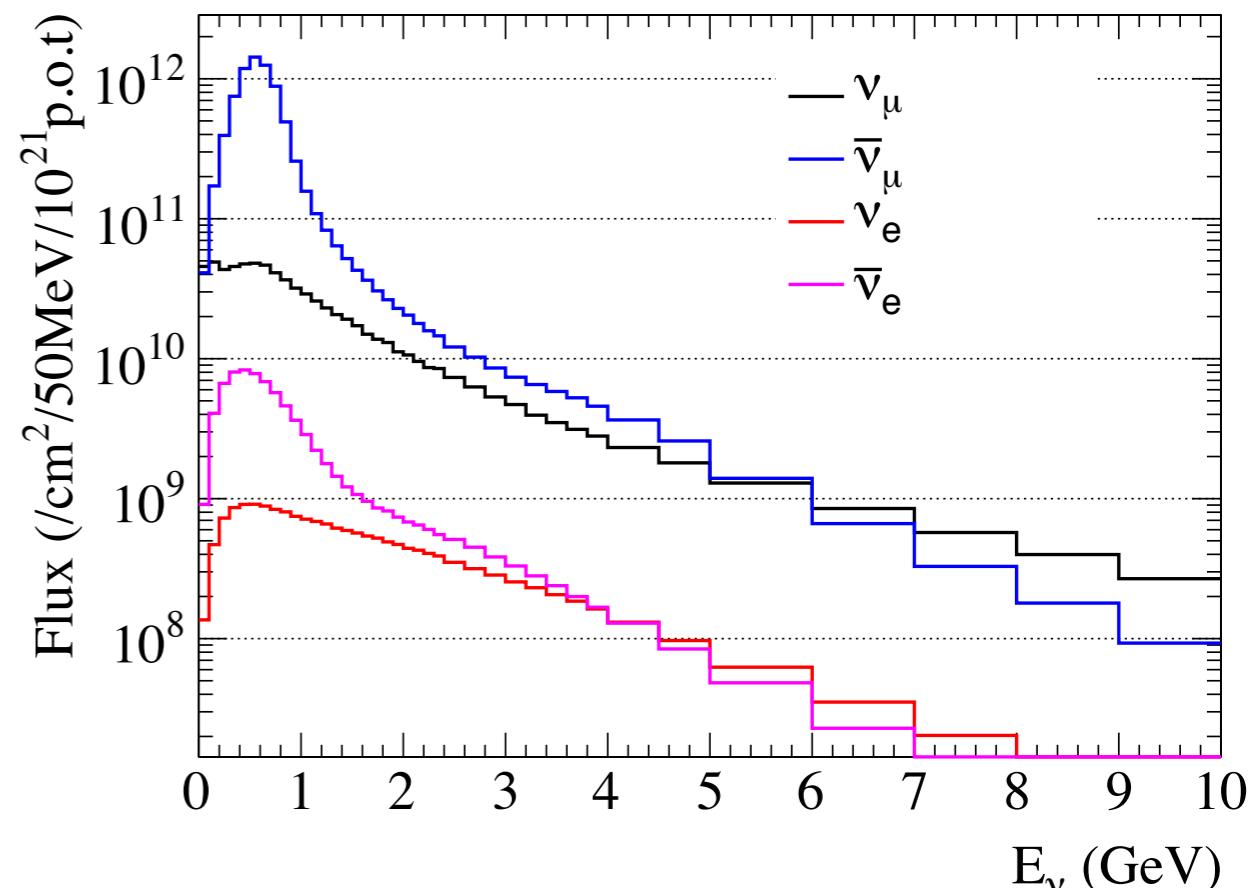
Dominant Reaction: CCQE  
Single Pion Production

# Flux at ND280

Neutrino Mode Flux at ND280



Antineutrino Mode Flux at ND280



In neutrino-mode

ν<sub>μ</sub> : ⟨E⟩ = 0.85 GeV, (~90%)

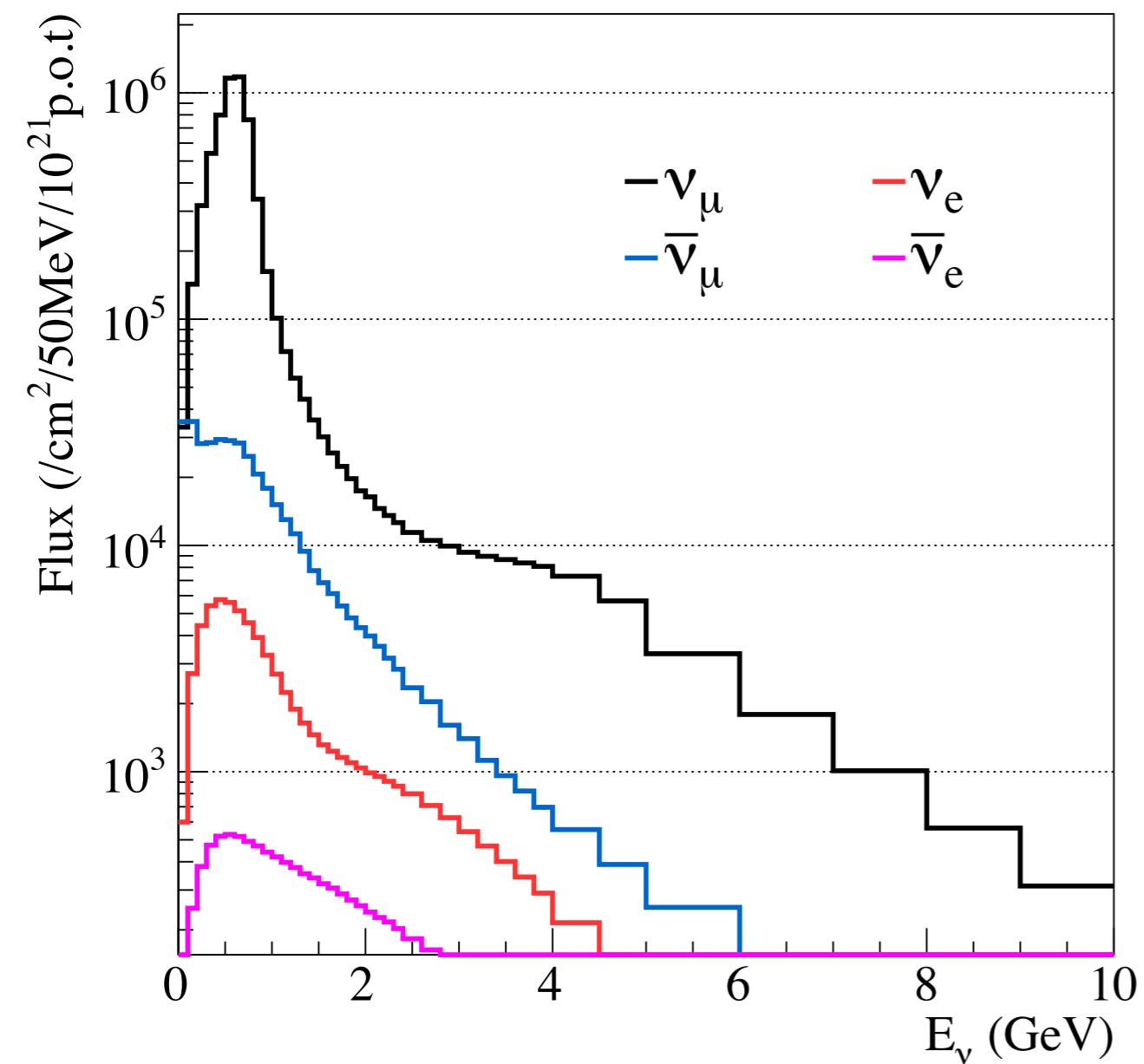
ν<sub>e</sub> : ⟨E⟩ = 1.3 GeV, (~1%)

Dominant Reaction: CCQE  
Single Pion Production

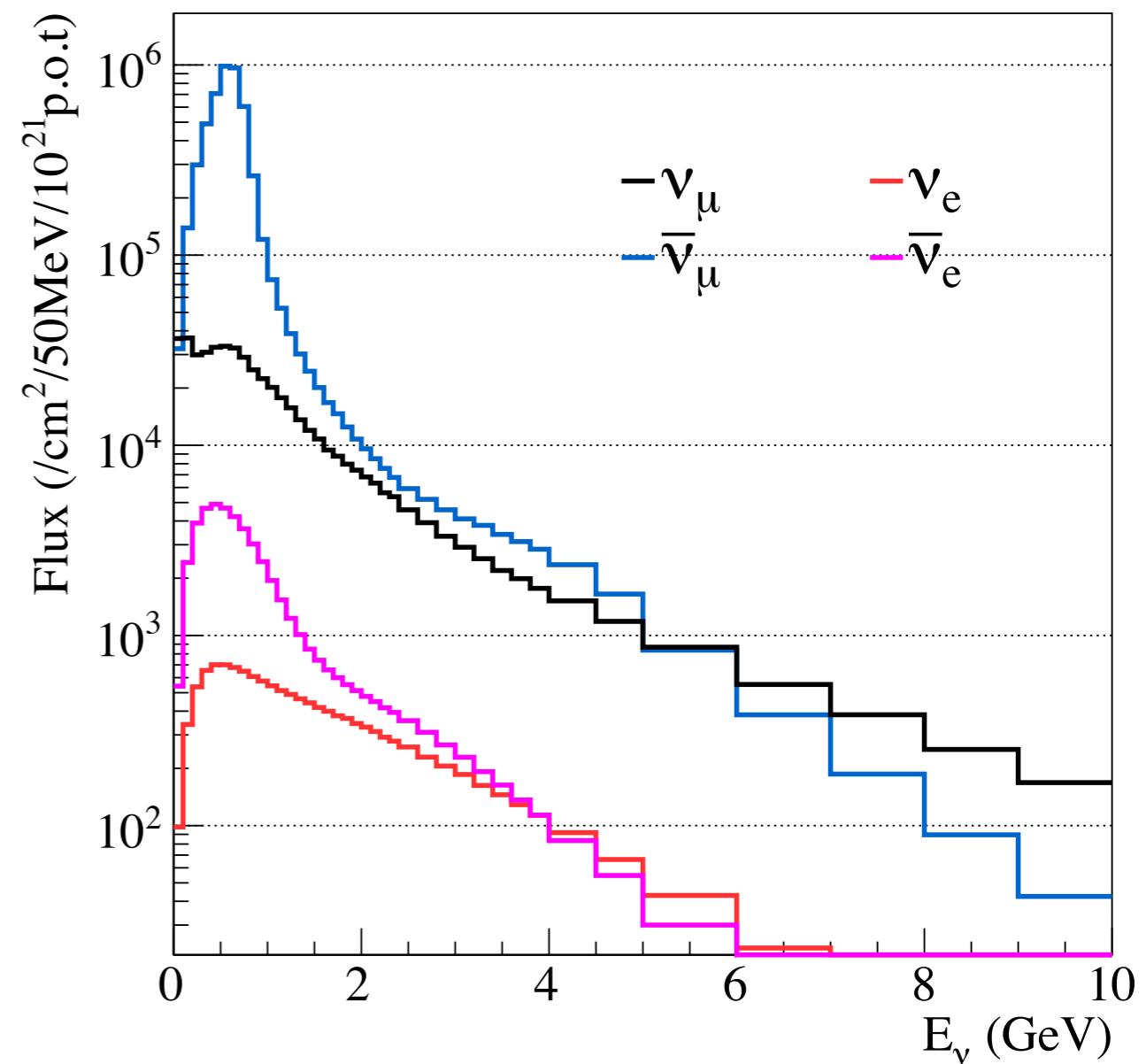
# Flux at Super-K

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Neutrino Mode Flux at SK

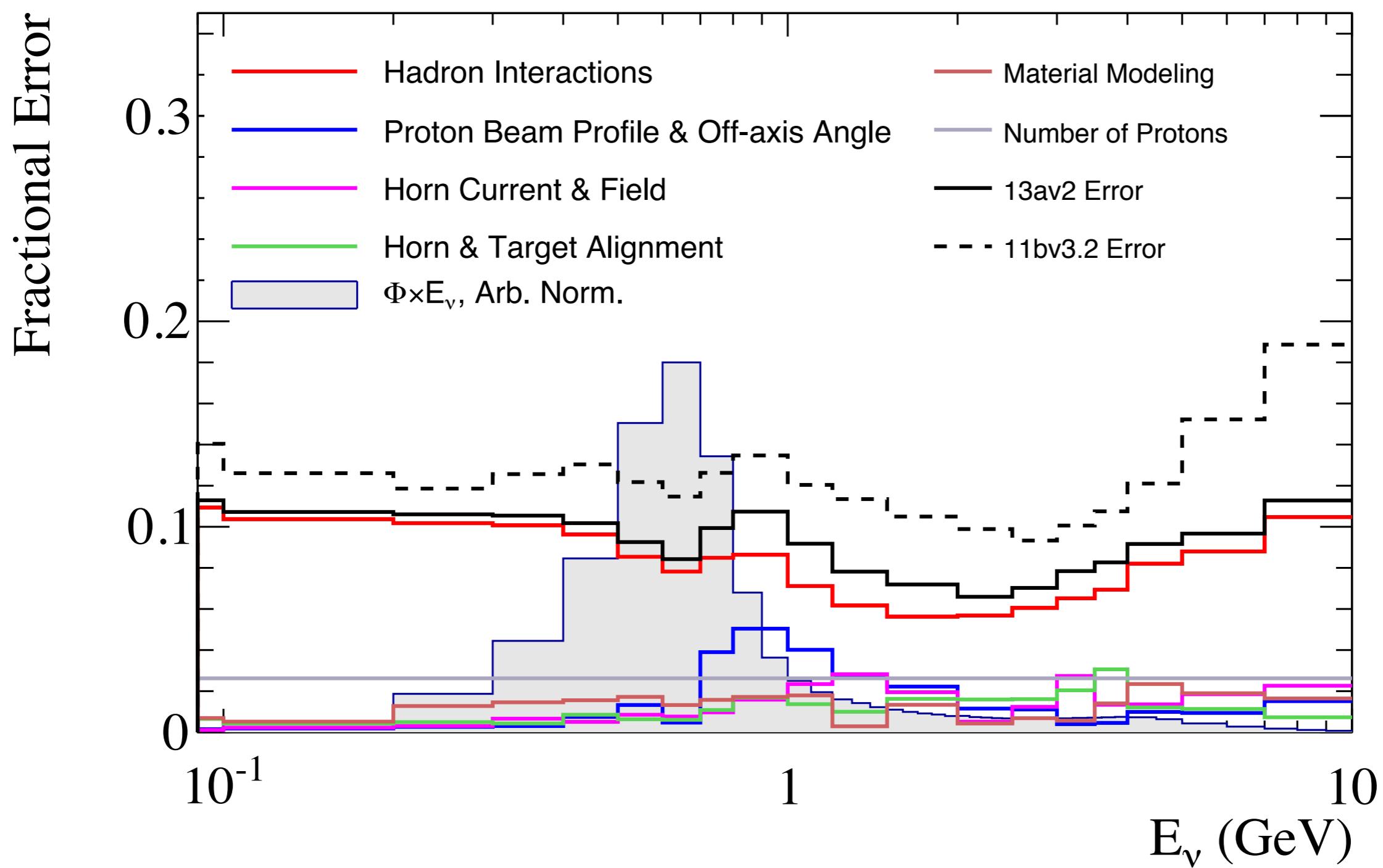


Antineutrino Mode Flux at SK

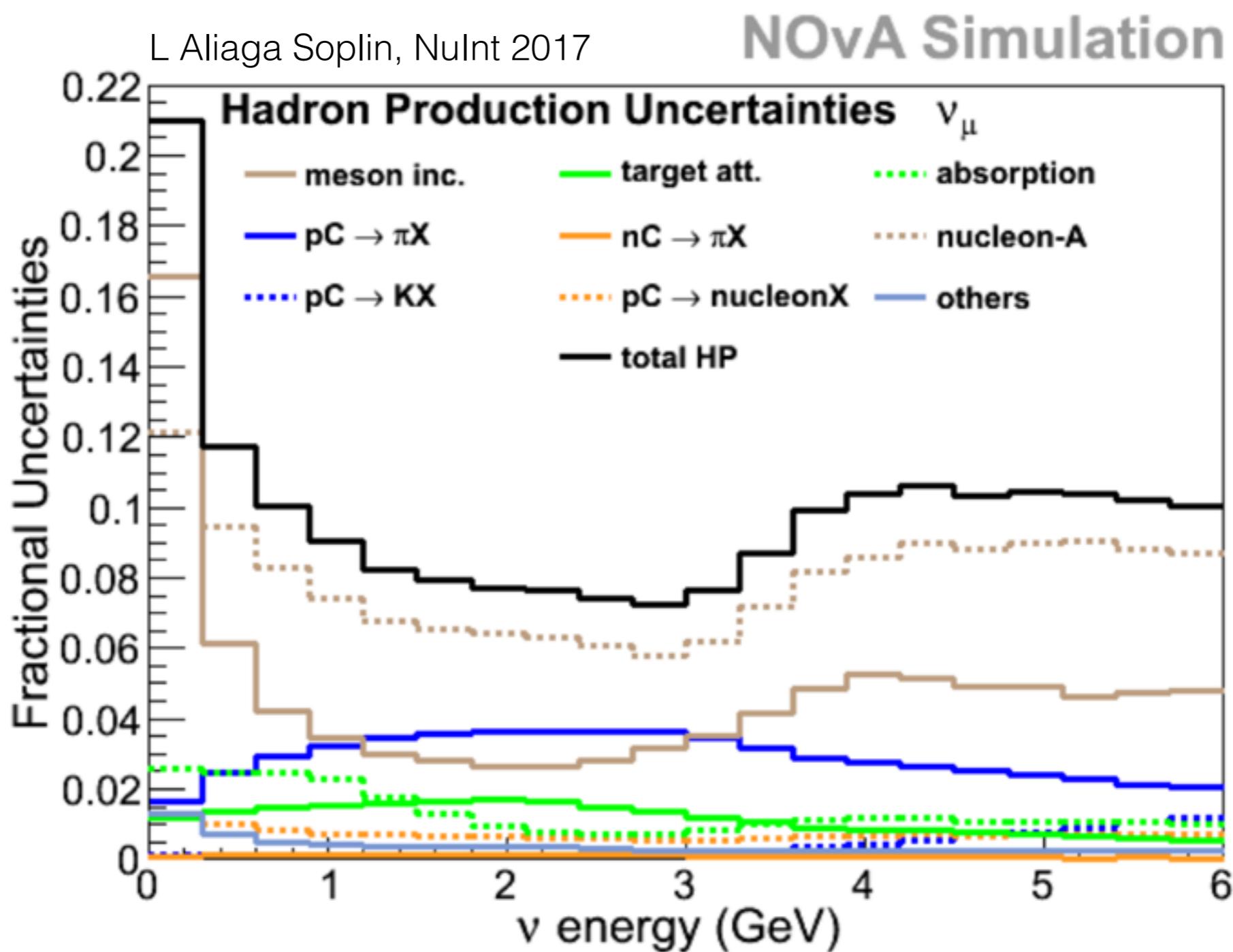


# Flux Uncertainty

SK: Neutrino Mode,  $\nu_\mu$

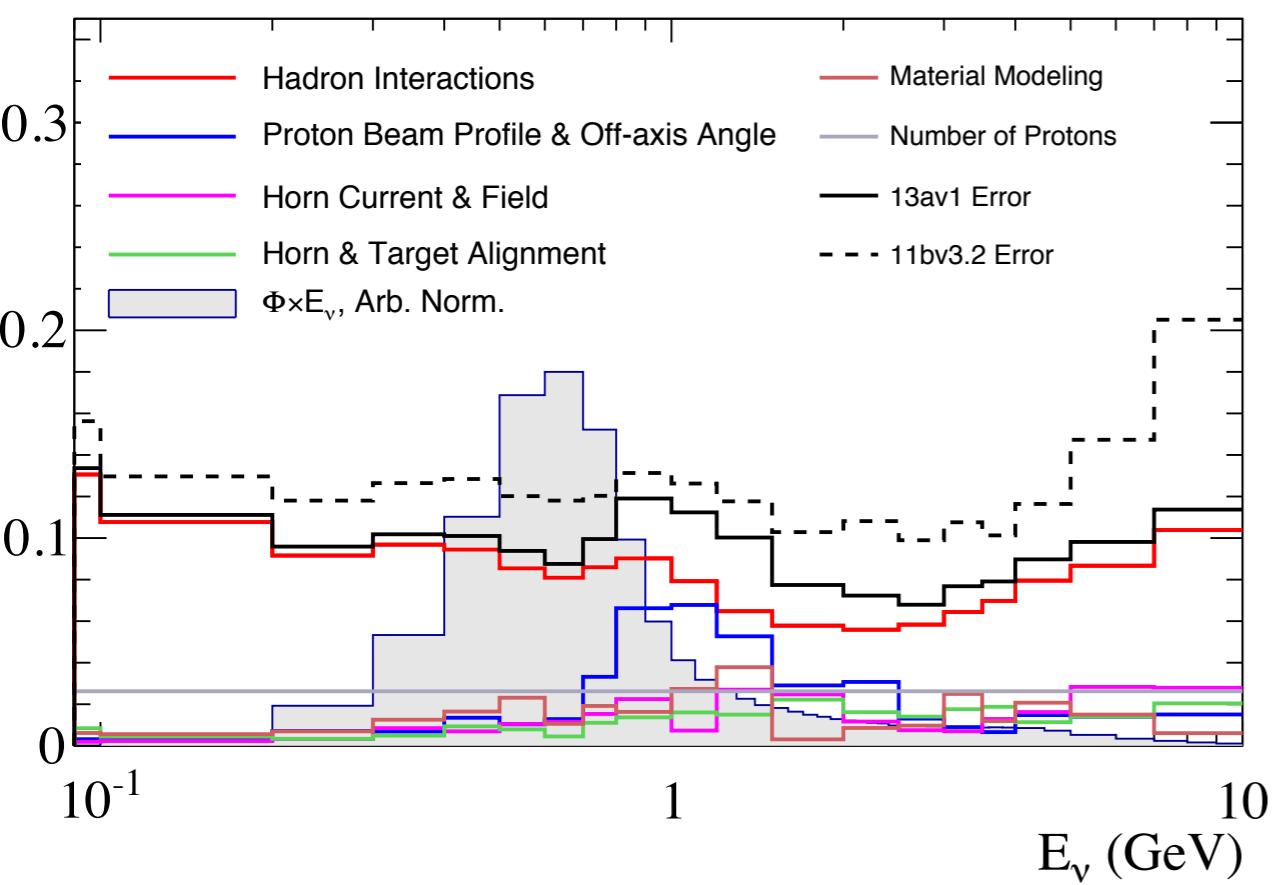


# Flux Uncertainty

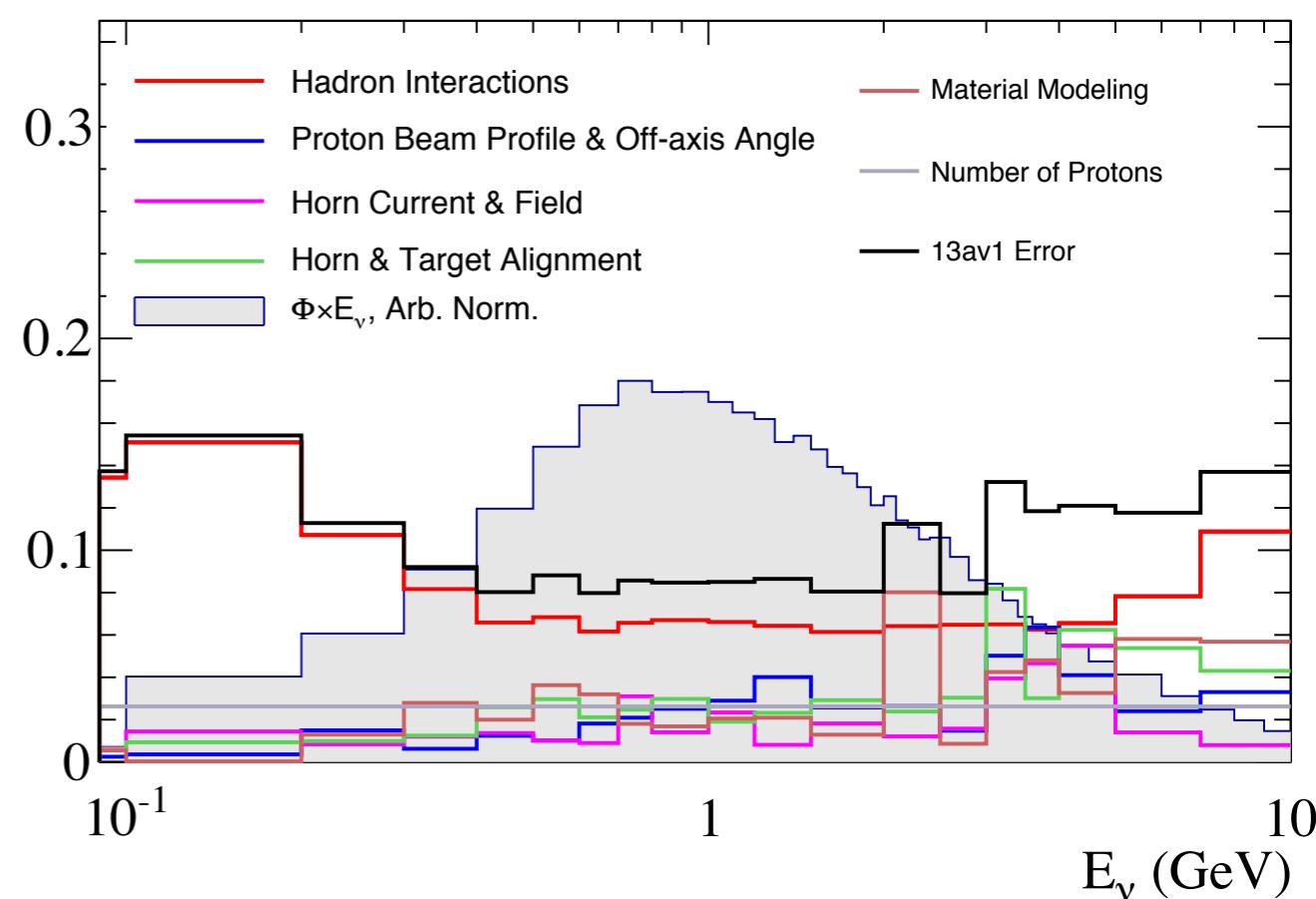


# Flux at ND280

ND280: Neutrino Mode,  $\nu_\mu$

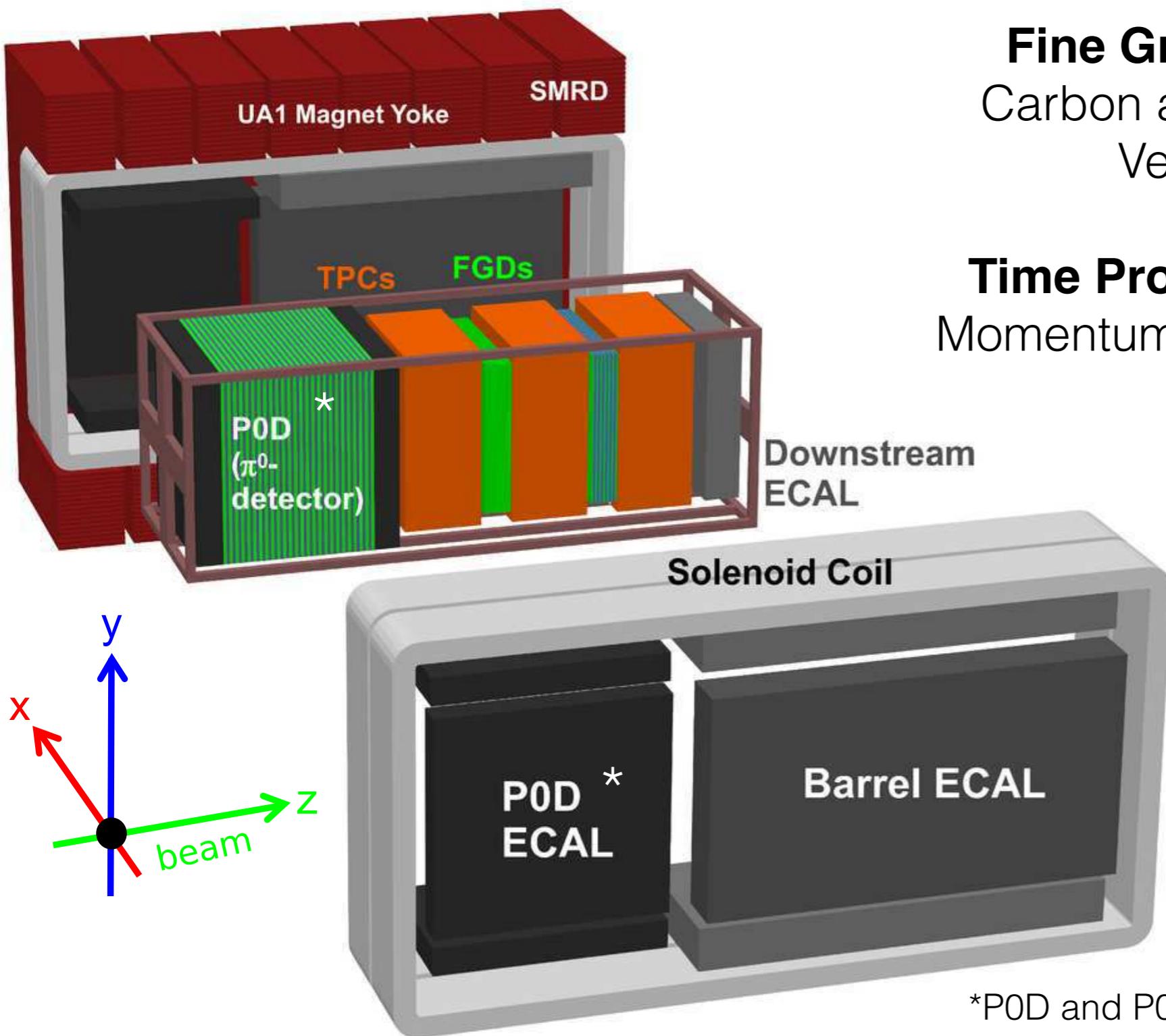


ND280: Antineutrino Mode,  $\bar{\nu}_\mu$



# ND280 Detector

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## Fine Grained Detectors (FGD)

Carbon and Oxygen Target Mass,  
Vertex reconstruction

## Time Projection Chambers (TPC)

Momentum and Charge Measurement  
Particle ID

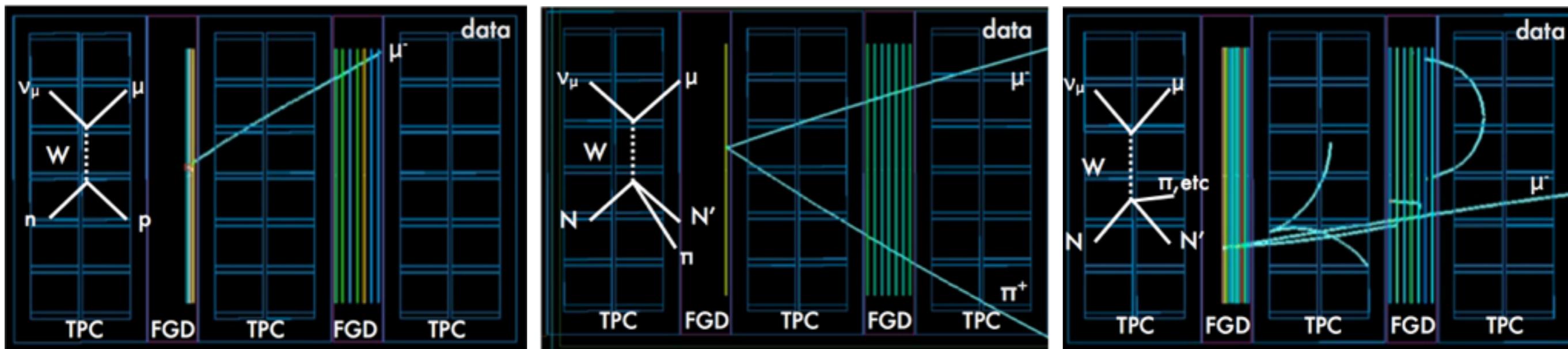
## EM Calorimeters

Neutral Particle Reconstruction  
Additional PID and  
energy measurement  
Tag entering backgrounds

\*P0D and P0D ECal detectors not be discussed here.

See arXiv:1111.5030 and arXiv:1308.3445 for information on these detectors.

# ND280 Input to T2K Oscillation Analysis



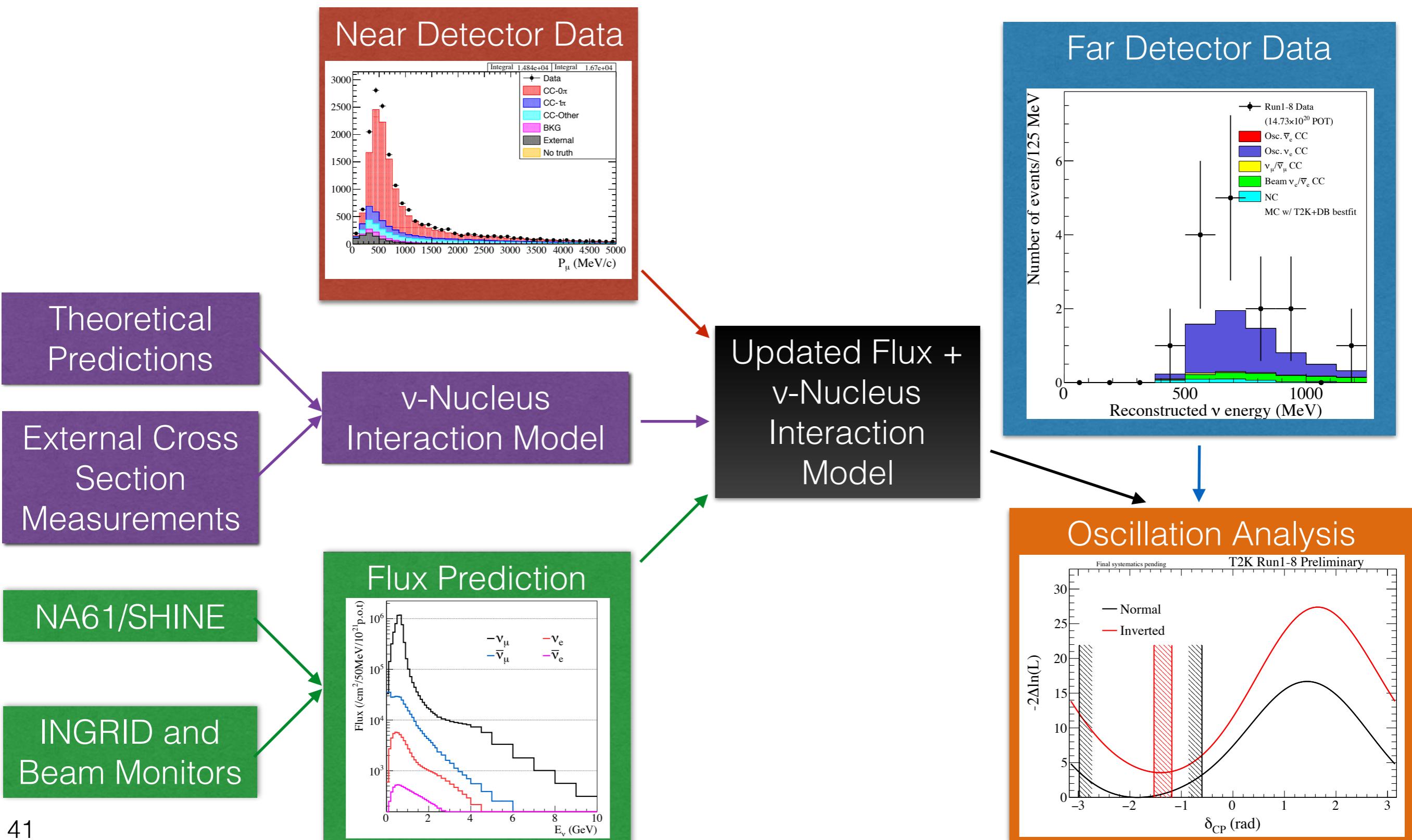
ND280 data split based on reconstructed topology enhanced in different interaction types

Fit flux + interaction model and propagate to far detector

As statistics increase and analysis becomes more sophisticated incorporate more channels

# T2K Analysis Strategy

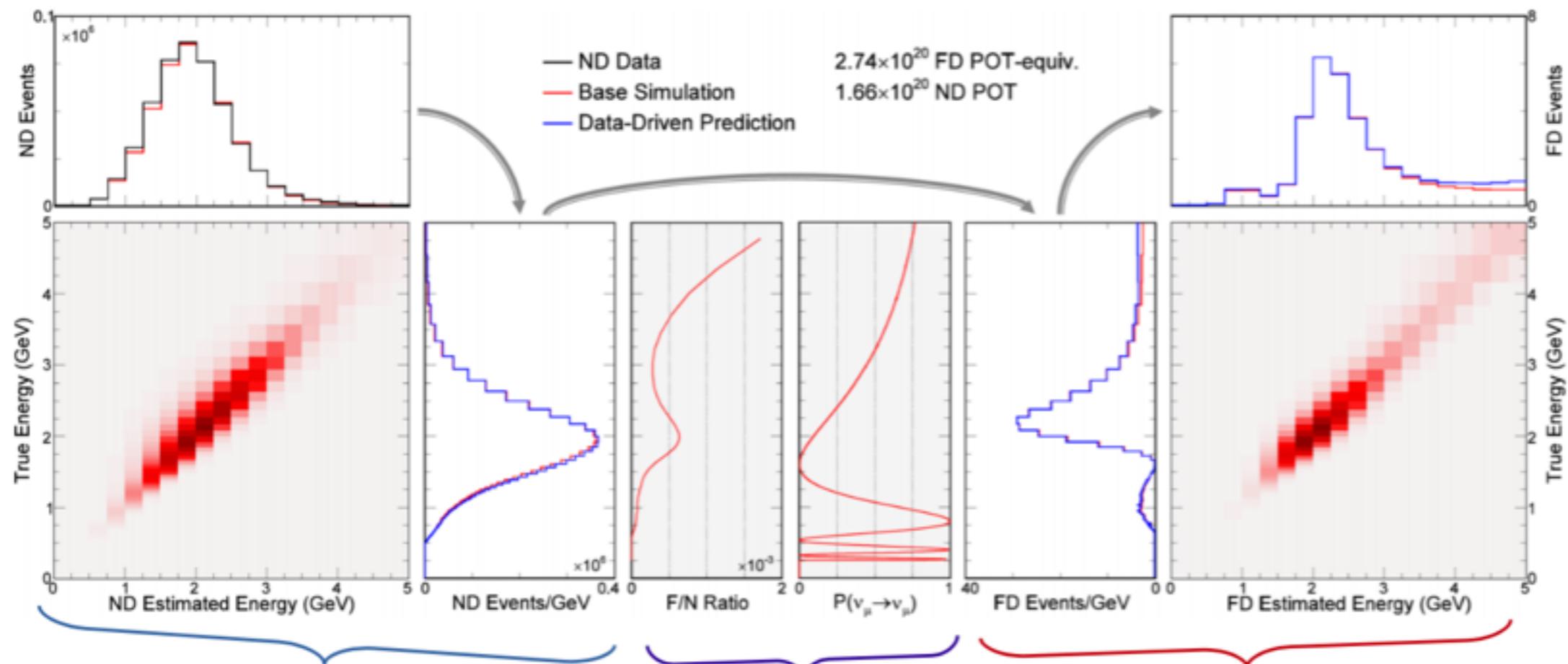
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# NOvA Analysis Strategy

To produce a data-driven prediction at FD, based on ND:

J. Wolcot, Nulnt 2017



True energy distribution is corrected so that reconstructed data & MC agree at the ND...

...modified true energy distribution is propagated through predicted geometric beam dispersion & acceptance ratio, oscillations...

... and “extrapolated” reconstructed energy distribution computed to compare to data